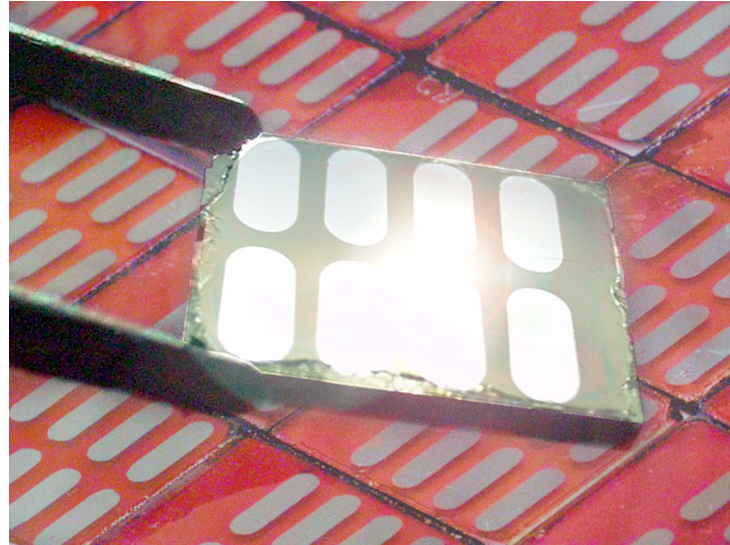


Ultrafast Dynamics of Excited Electrons in Materials for Energy Applications



Marco Bernardi

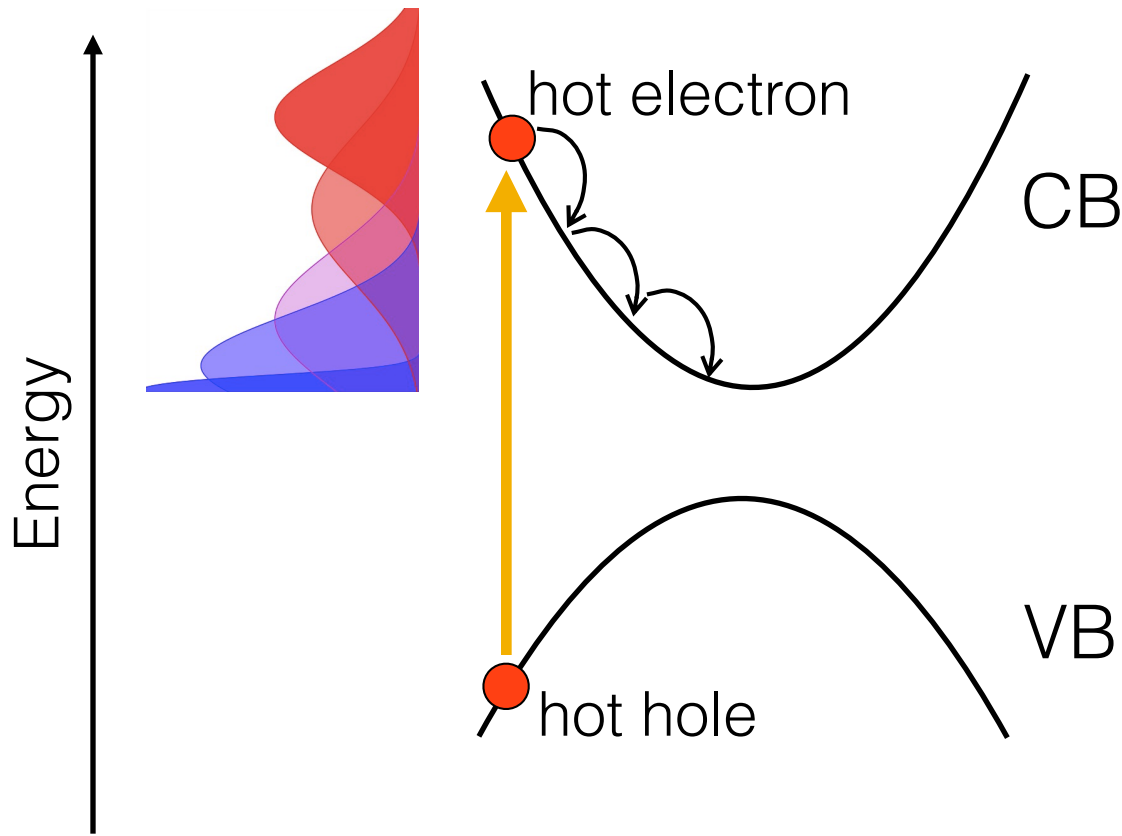
Physics Department, University of California at Berkeley



E-mail: bmarco@civet.berkeley.edu

Web: www.bernardilab.com

Ultrafast Dynamics of Excited Carriers

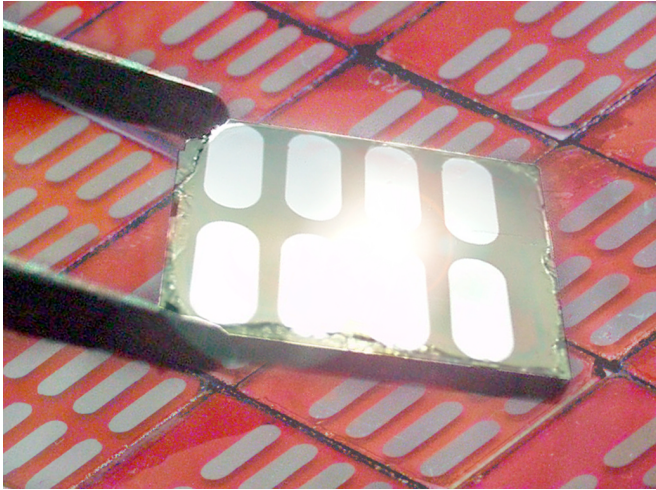


Understand hot carriers in materials:

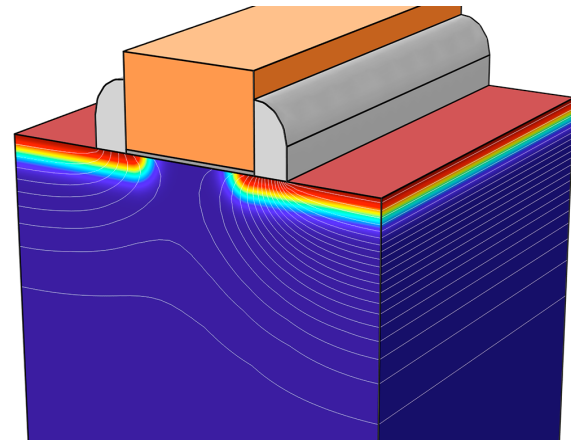
- Energy distribution vs. time
- Timescale (10–100 fs) for energy loss
- Transport and mean free paths

Hot Carriers in Science and Technology

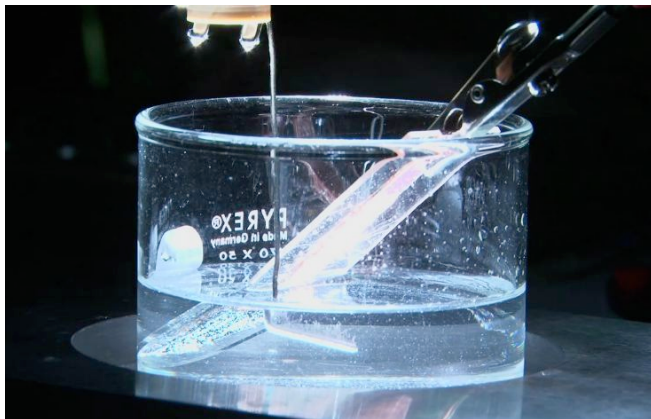
Solar Cells



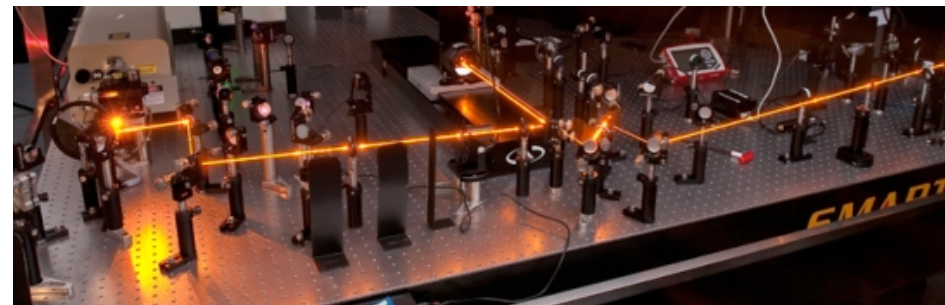
Electronics



Photocatalysis



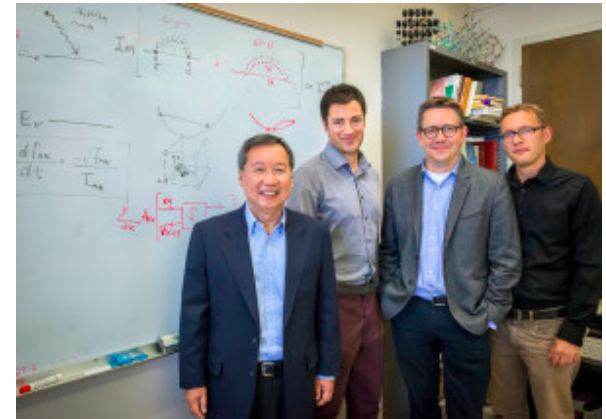
Ultrafast spectroscopy



Hot Carriers from First Principles

First Ab Initio Method for Characterizing Hot Carriers Could Hold the Key to Future Solar Cell Efficiencies

Science Shorts Lynn Yarris (mailto:lcyarris@lbl.gov) • JULY 17, 2014



(<http://newscenter.lbl.gov/wp-content/uploads/sites/2/2014/07/Steve-Louie-and-Jeff-Neaton.jpg>)

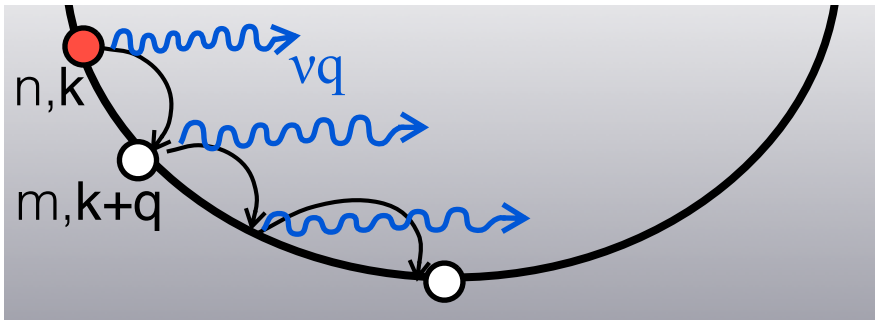
Work with Steve Louie and Jeff Neaton (UC Berkeley)

- 1) Computational approach
- 2) Hot carriers in Silicon and GaAs
- 3) Hot carriers from surface plasmons in Au and Ag

Hot Carrier Scattering

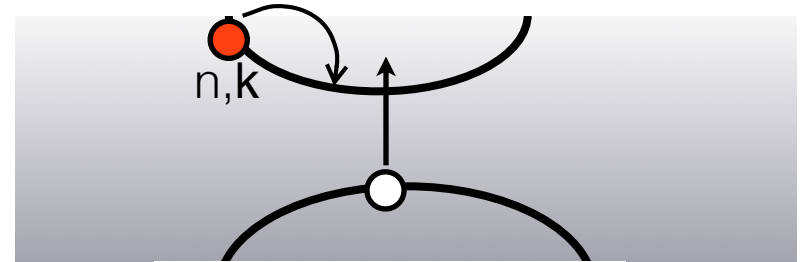
Two ultrafast (<1ps) mechanisms for hot carriers to lose energy

Electron – phonon scattering

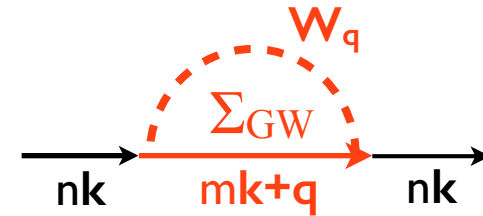
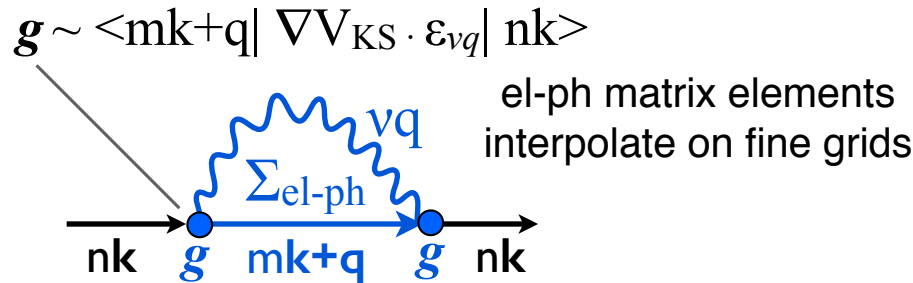


Electron – electron scattering

“Impact ionization” & Auger processes



Use perturbation theory



$$(\tau_{nk}^{-1})_{el-ph} \sim \text{Im}(\Sigma_{nk})_{el-ph} = \text{Im} g^2 G D$$

Quantum Espresso + EPW code

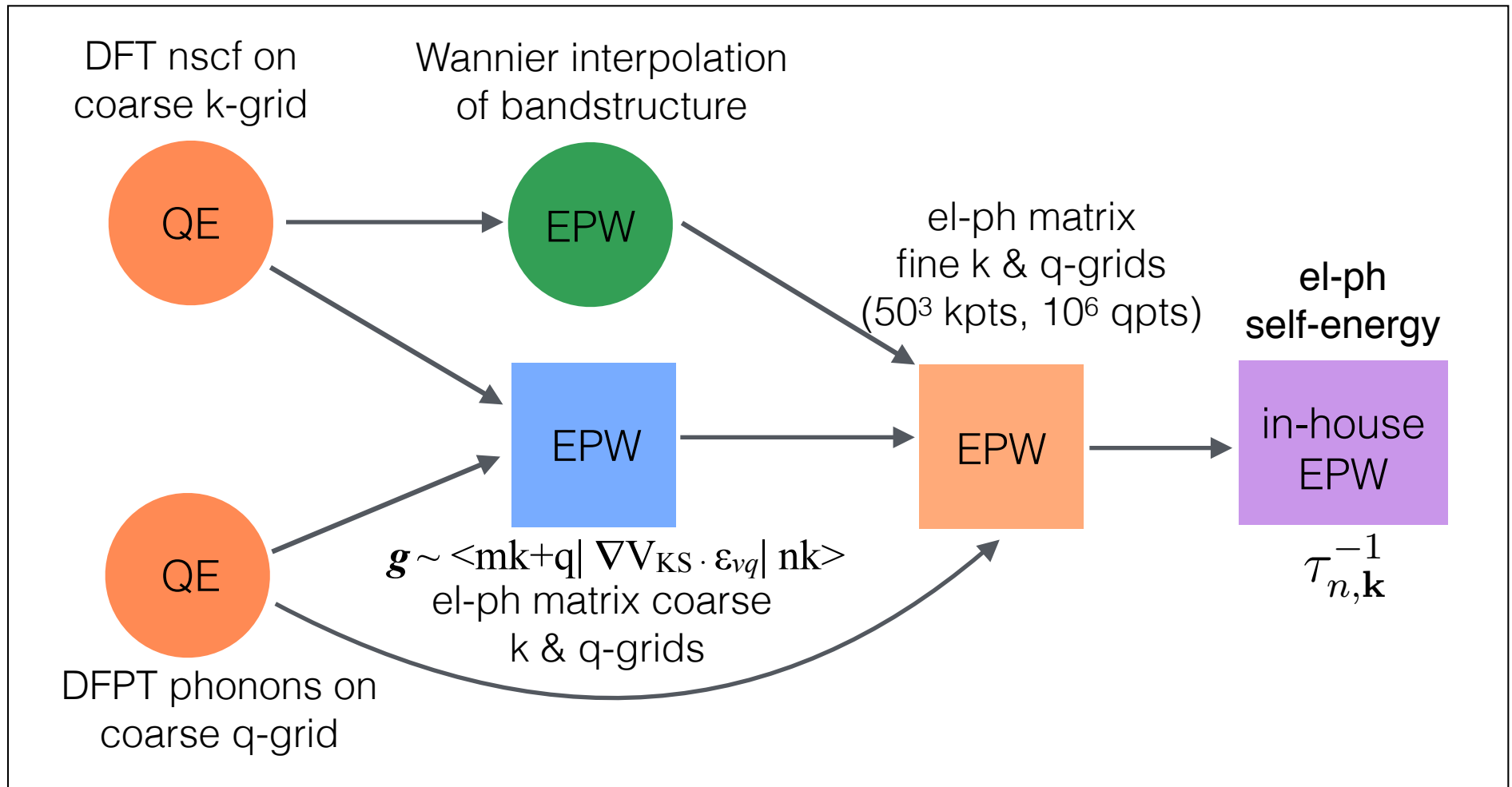
$$(\tau_{nk}^{-1}) \sim \text{Im}(\Sigma_{nk})_{el-el} = \text{Im} G \cdot (\epsilon_{RPA}^{-1} V)$$

Quantum Espresso + Berkeley GW

Relaxation time of carrier in state n, k

$$(\tau_{nk})^{-1} = \text{Im}(\Sigma_{nk})_{el-ph} + \text{Im}(\Sigma_{nk})_{el-el}$$

Workflow for Electron-Phonon Calculation



el-ph matrix elements

5-dim array

$$\tau_{n\mathbf{k}}^{-1} = \frac{2\pi}{\hbar} \frac{1}{N_{\mathbf{q}}} \sum_{m,\nu,\mathbf{q}} |g_{nm\mathbf{k}}^{\nu\mathbf{q}}|^2 \left[\underbrace{(N_{\nu\mathbf{q}} + 1 - f_{m,\mathbf{k}+\mathbf{q}})}_{\text{Lorentzian 10 meV broadening}} \delta(\epsilon_{n\mathbf{k}} - \epsilon_{m,\mathbf{k}+\mathbf{q}} - \hbar\omega_{\nu\mathbf{q}}) + (N_{\nu\mathbf{q}} + f_{m,\mathbf{k}+\mathbf{q}}) \delta(\epsilon_{n\mathbf{k}} - \epsilon_{m,\mathbf{k}+\mathbf{q}} + \hbar\omega_{\nu\mathbf{q}}) \right]$$

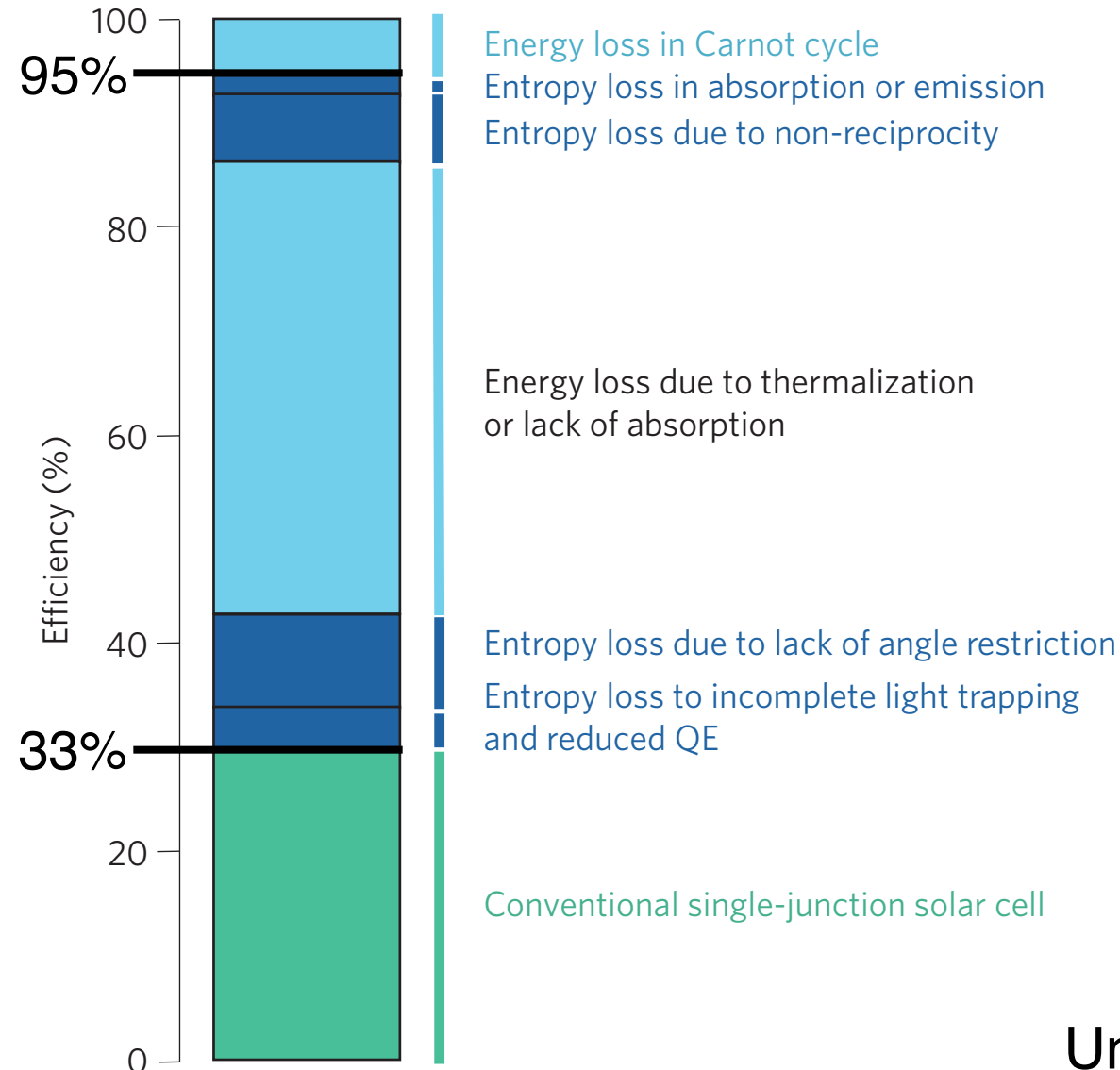
Lorentzian 10 meV broadening

random q-grid

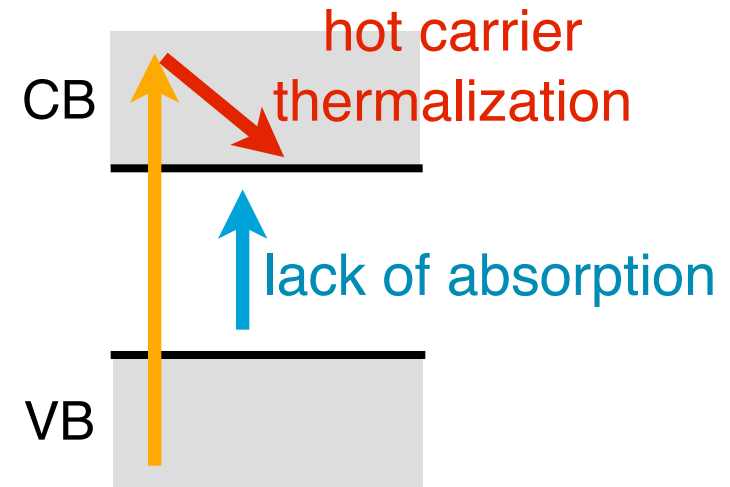
“Monte Carlo” integration

Thermalization Loss in Solar Cells

Shockley-Queisser efficiency limit for a single-junction solar cell: ~33%



Two main losses in PV

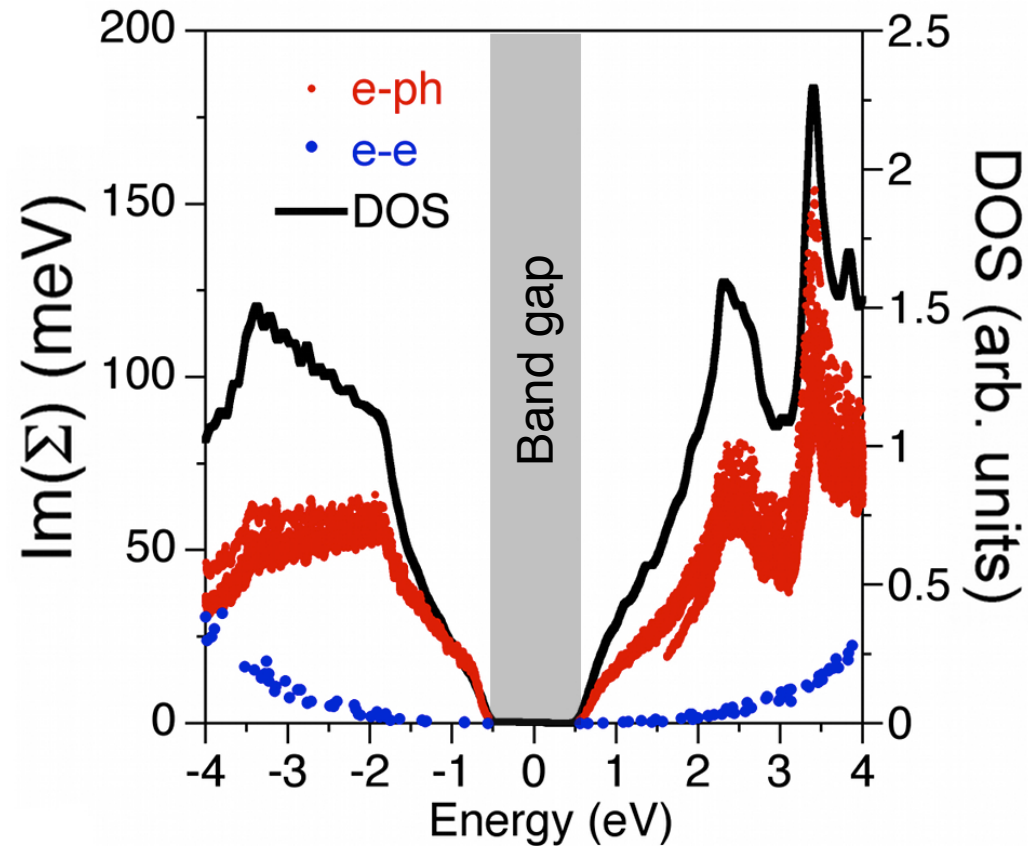


Absorption loss ~20%

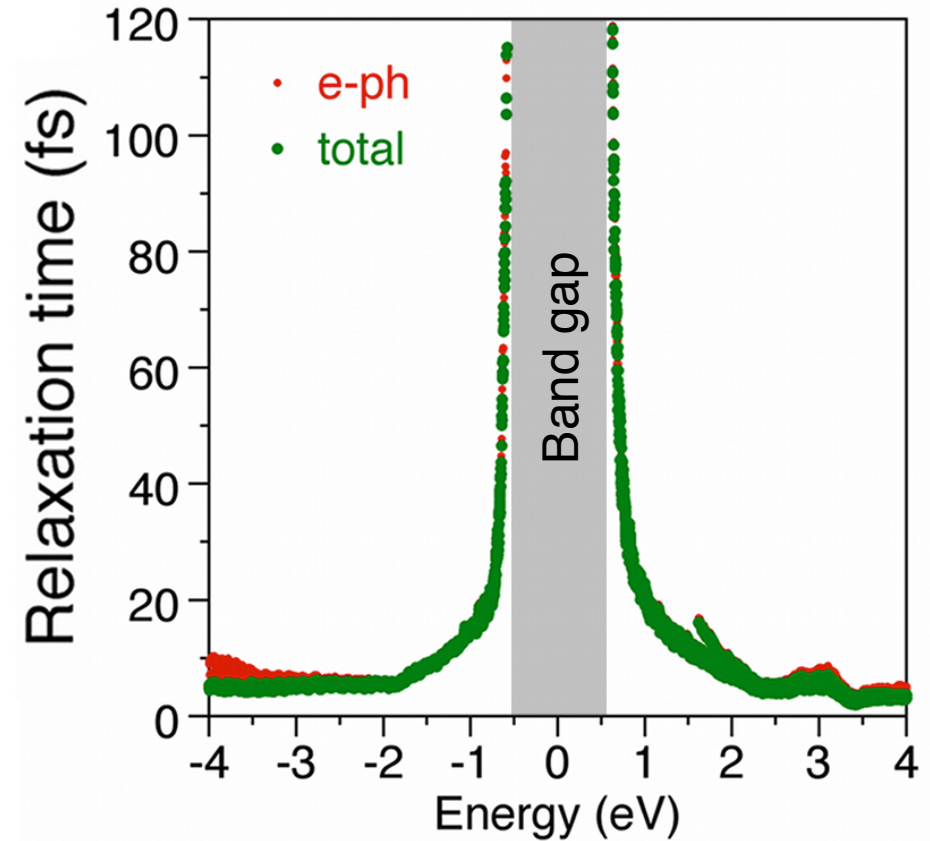
Thermalization loss ~25%

Understand ultrafast (sub-ps) loss of solar energy from first principles

Hot Carrier Relaxation Times in Silicon



El-ph scattering dominates thermalization
El-ph scattering rate \sim electronic DOS

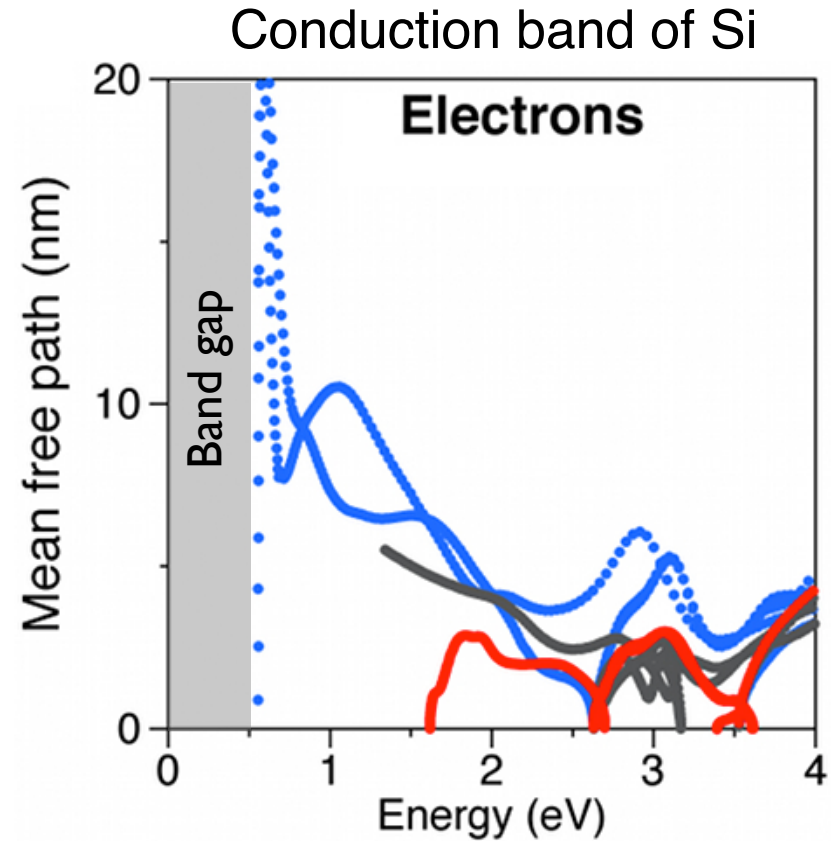
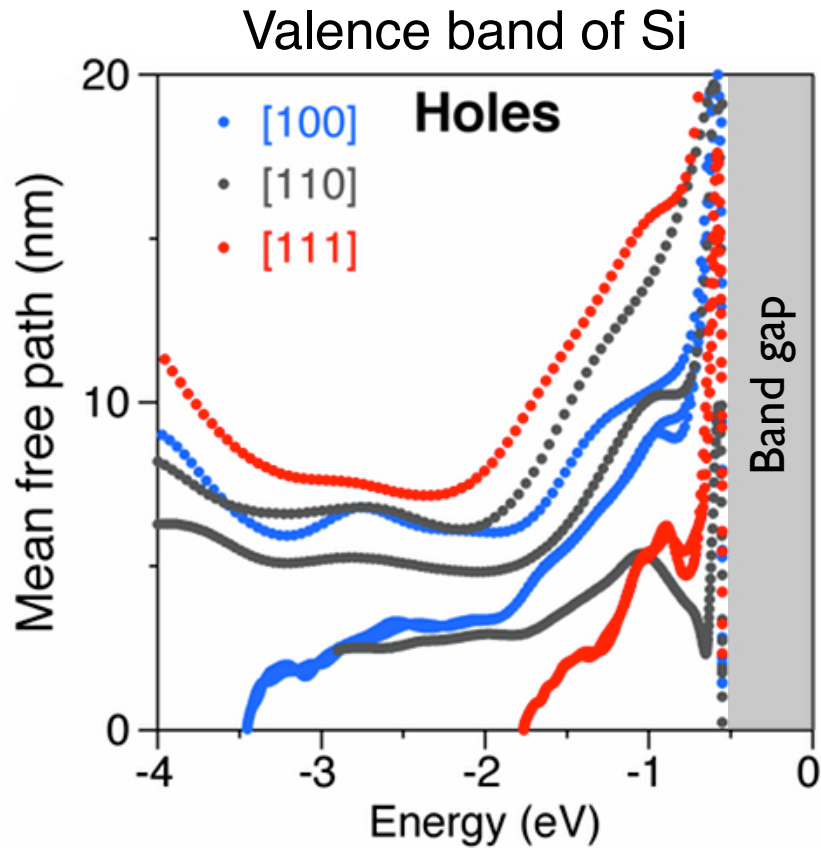


Fast relaxation away from band edge: ~ 10 fs
Slower relaxation near the band edge: > 100 fs

Mean Free Paths

Distance hot carriers can travel before emitting a phonon

$$\text{Mean free path: } L_{n,\vec{k}} = v_{n,\vec{k}} \cdot \tau_{n\vec{k}}$$



Mean free path \sim 5–10 nm in Si

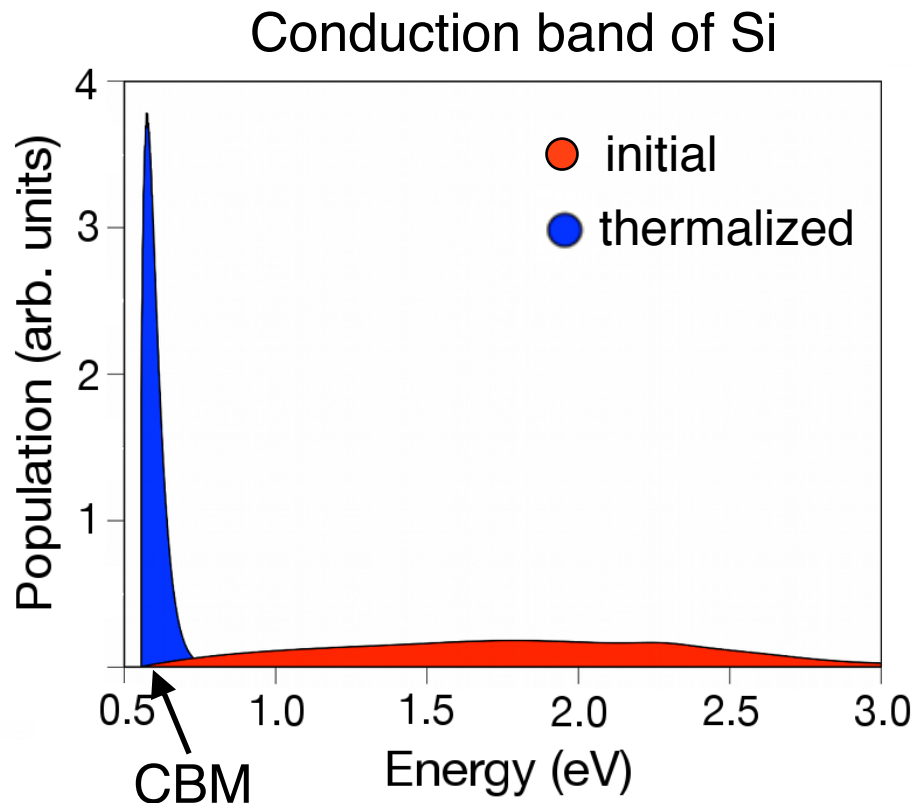
[100] direction favorable for hot electron extraction

The First Picosecond after Sunlight Absorption in Silicon

Initial population at $t=0$ under AM1.5 solar illumination

$$f(E, t = 0) \propto \int_0^{4 \text{ eV}} \underbrace{d\omega D(E - \omega)}_{\text{Electron DOS}} \cdot \underbrace{J_{ph}(\omega)}_{\text{AM1.5 photon flux}} \cdot \underbrace{\alpha(\omega)}_{\text{Experimental absorption}}$$

Thermalized population at $t \approx 1$ ps: Fermi-Dirac at $T=300\text{K}$ ($\sim 10^{17} \text{ cm}^{-3}$ carriers)



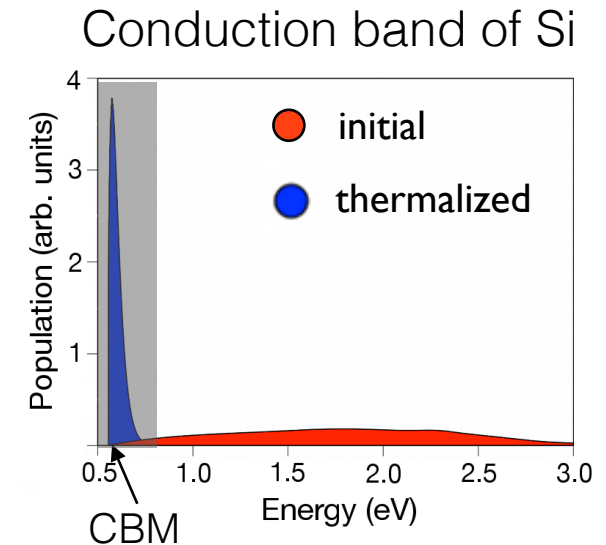
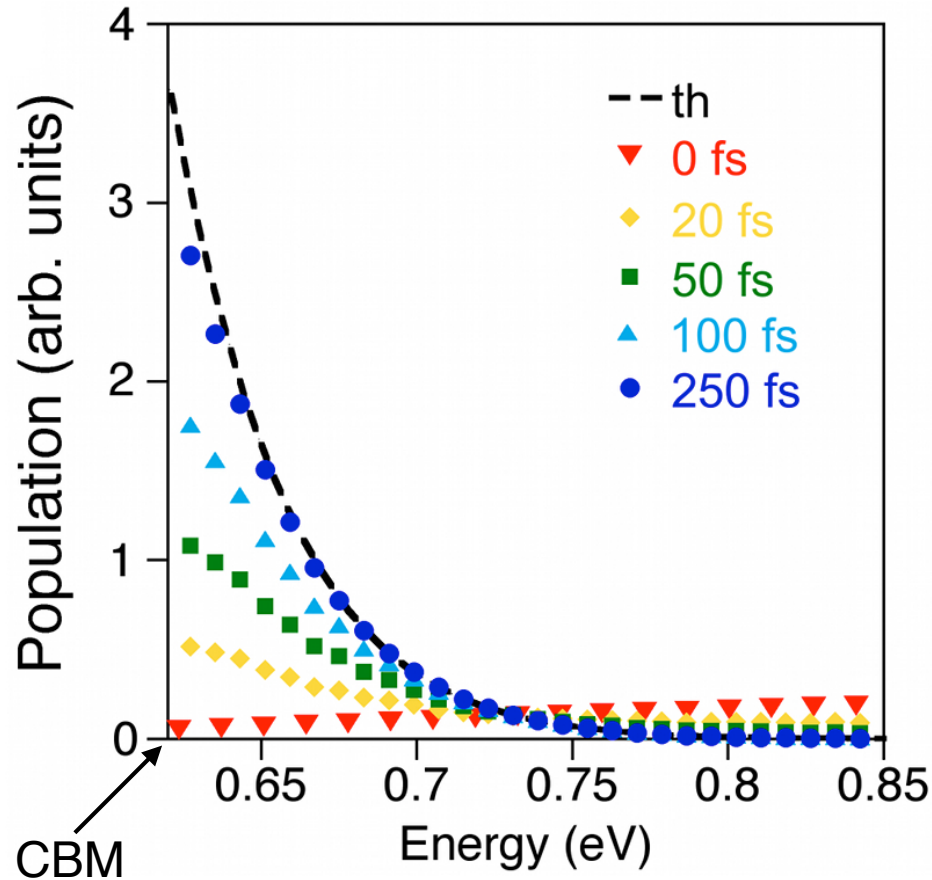
Carrier Dynamics

Boltzmann equation
for carrier in state n, \mathbf{k}

$$\frac{df_{n,\mathbf{k}}(t)}{dt} = -\frac{f_{n,\mathbf{k}}(t) - f_{n,\mathbf{k}}(t_{th})}{\tau_{n,\mathbf{k}}}$$

The First Picosecond after Sunlight Absorption in Silicon

Hot electron thermalization near the conduction band minimum (CBM)



Excellent agreement with pump-probe experiments

Experiment: thermalization in ~250–300 fs near CBM

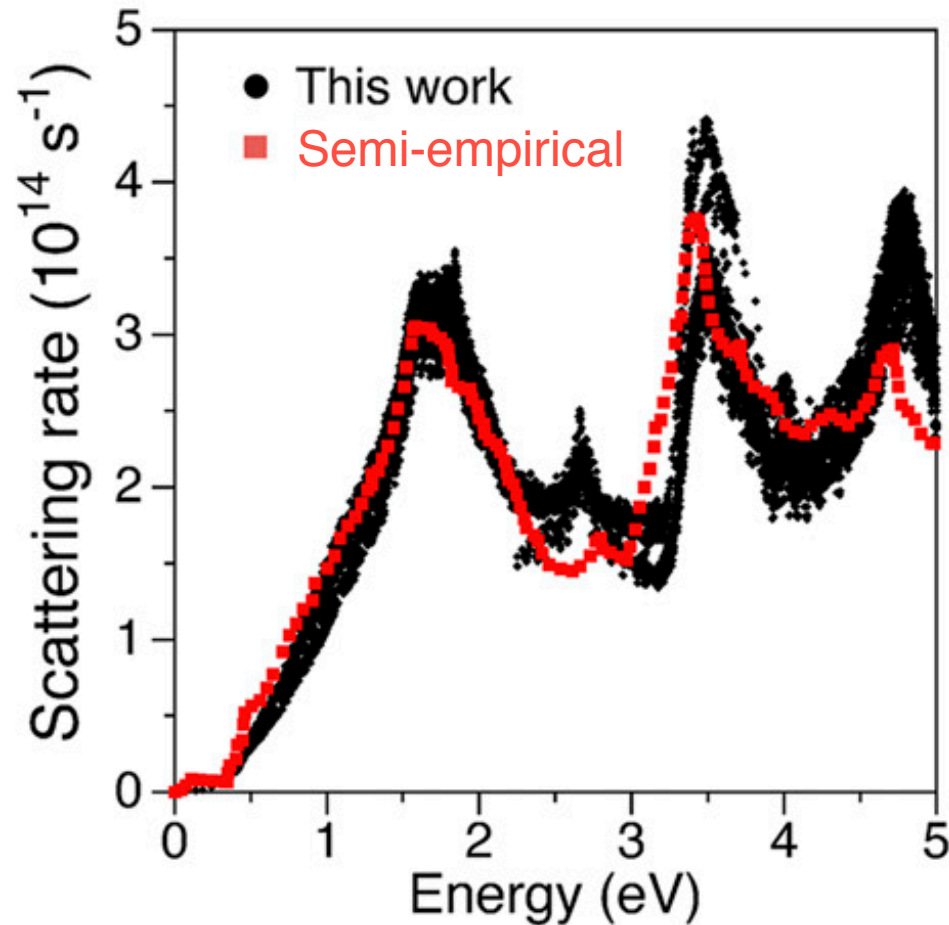
Model hot carriers and ultrafast spectroscopy

Hot Electrons in GaAs

Ab initio phonon and bandstructure calculations

Compute ~50 trillion el-ph matrix elements

No adjustable parameters in the calculation

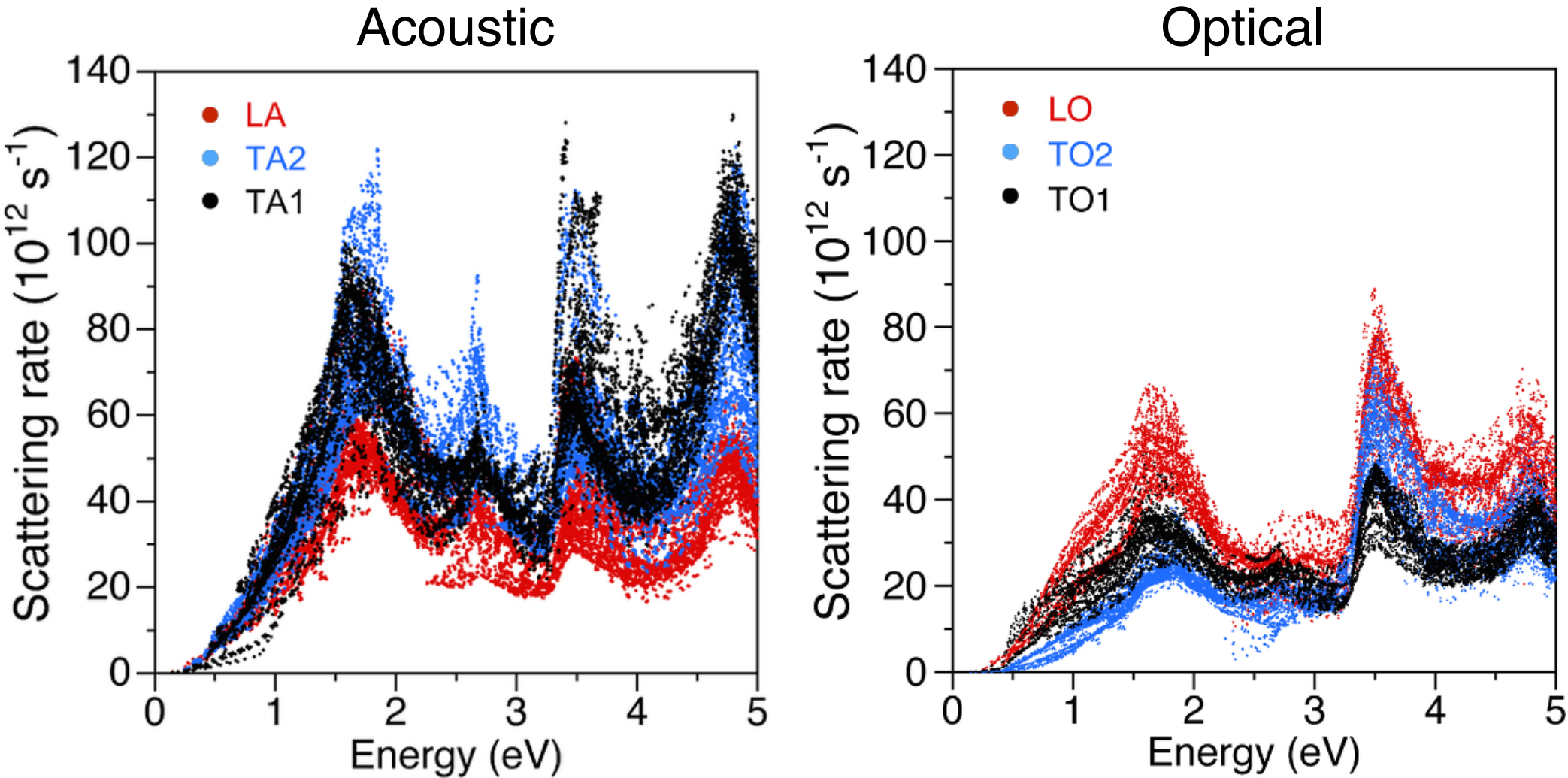


M. Fischetti, et al. Phys. Rev. B 38, 9721 (1988)

Multiple parameters for el-ph coupling (deformation potentials)

M. Bernardi et al., PNAS 112, 5291(2015)

GaAs – Mode Contributions

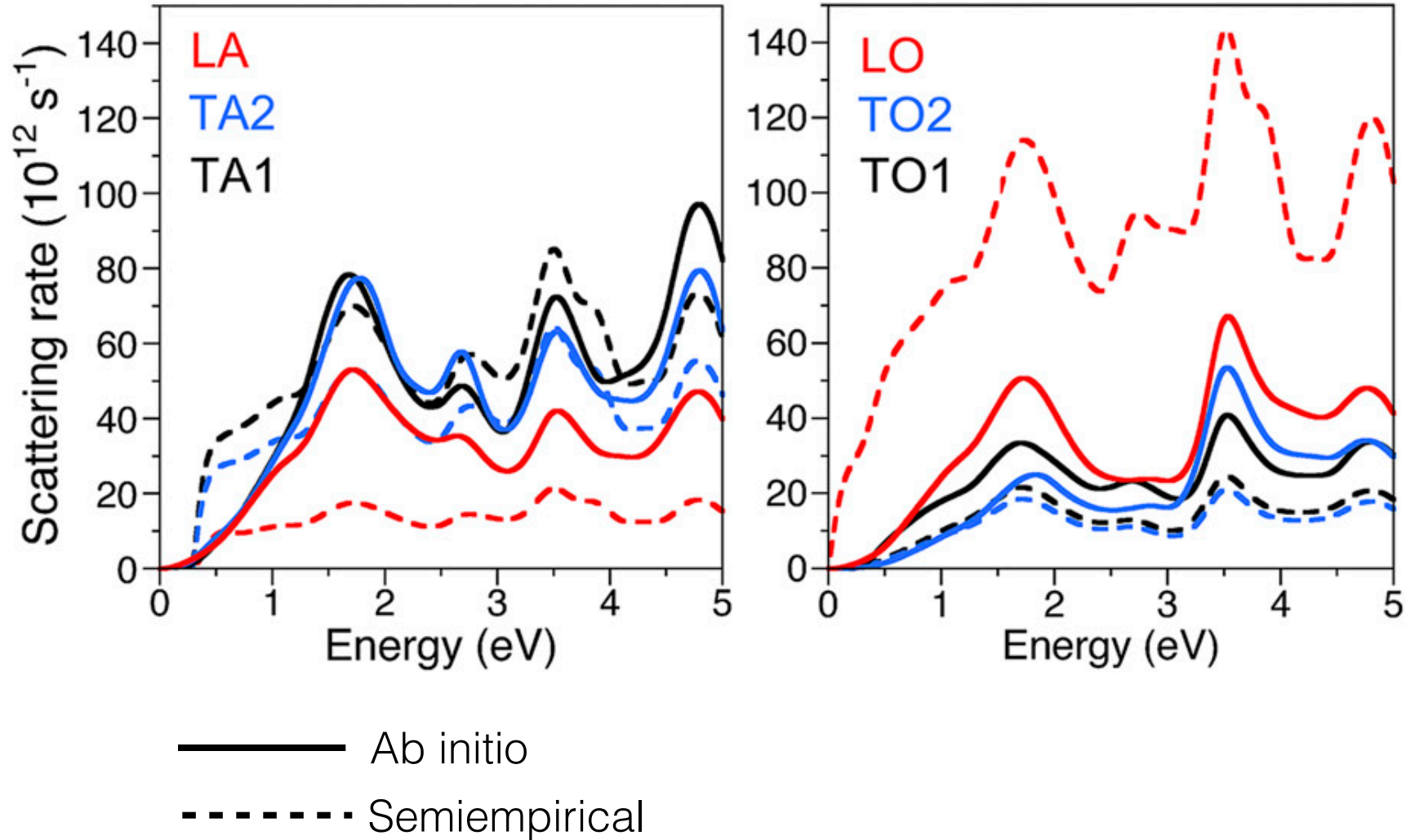


Acoustic modes dominate hot electron scattering (not LO!)

LO strongest among optical modes

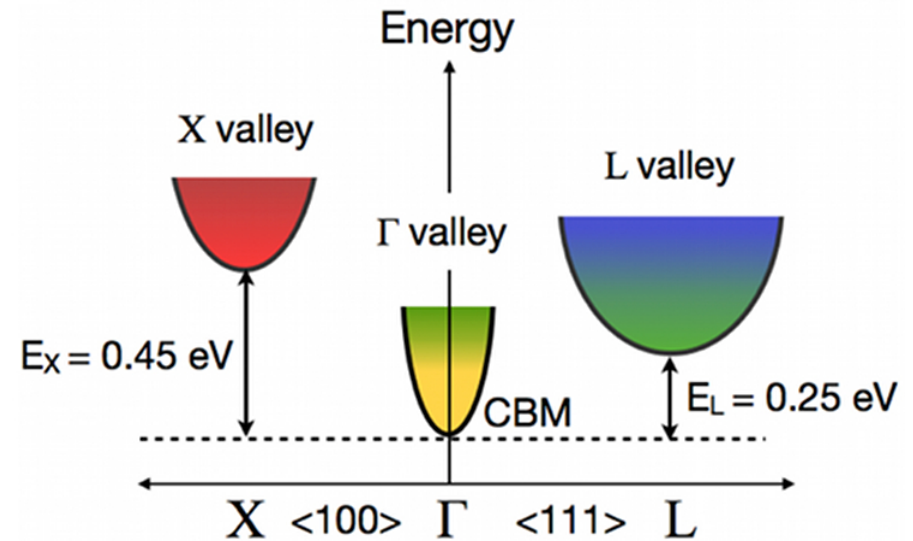
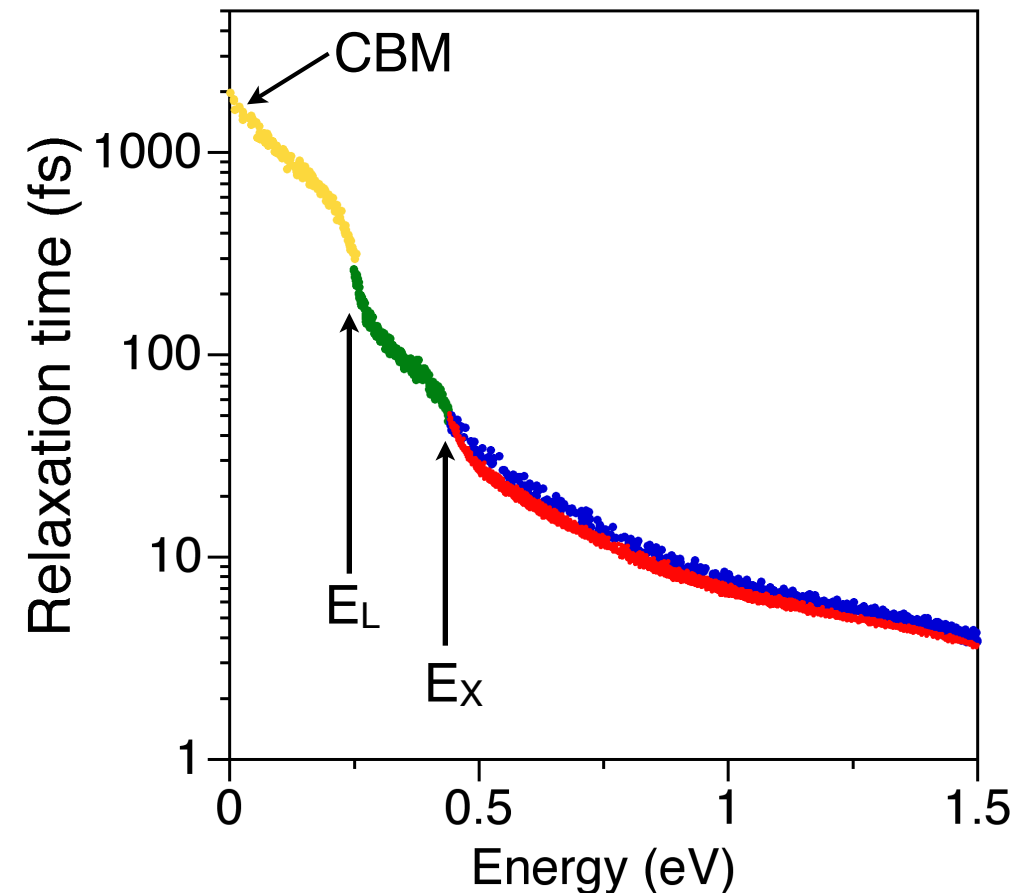
GaAs – Mode Contributions Comparison

Where did the “old” (semiempirical) calculations go wrong?



Hot Electron Thermalization in GaAs

Conduction band of GaAs



Each valley sampled with 200^3 k-grid

Excellent agreement with
pump-probe experiments

Help resolve a long-standing
controversy on HCs in GaAs

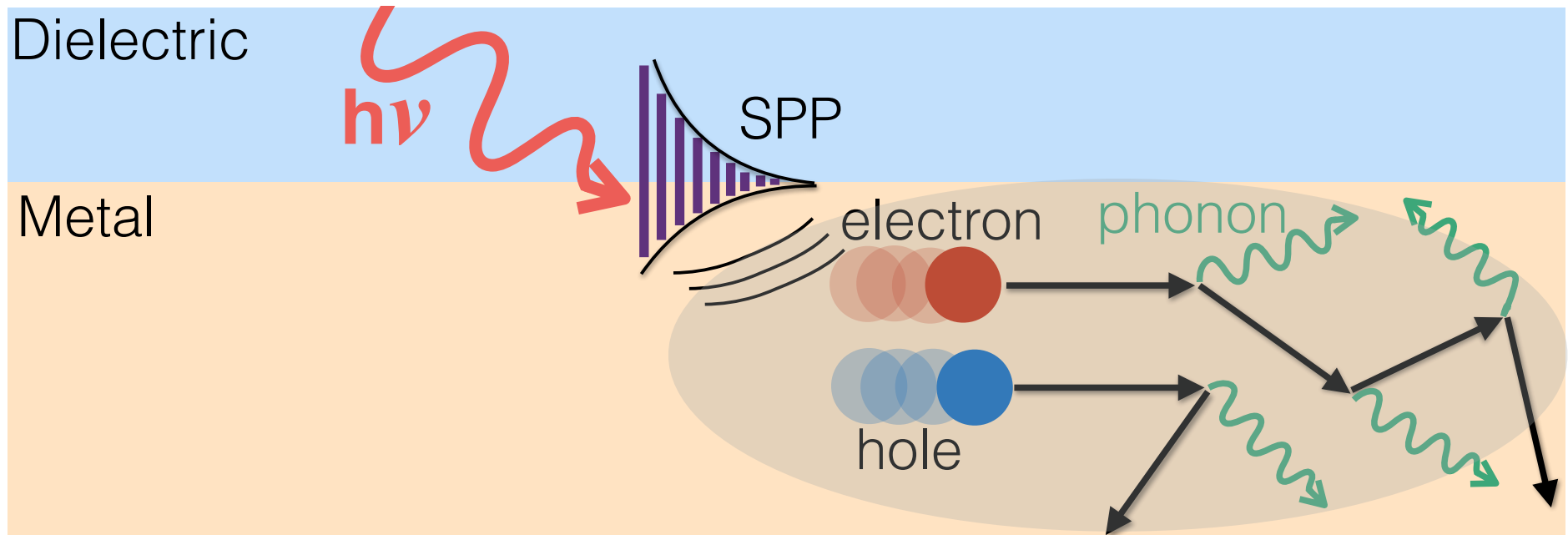
Experiment: pump with 2 eV light yields three
time decay signals: ~ 40 fs, ~ 200 fs, 1.5 ps

▬ ▬ ▬

Young, et al. *Phys. Rev. B* 50, 2208 (1994)

M. Bernardi et al., *PNAS* 112, 5291(2015)

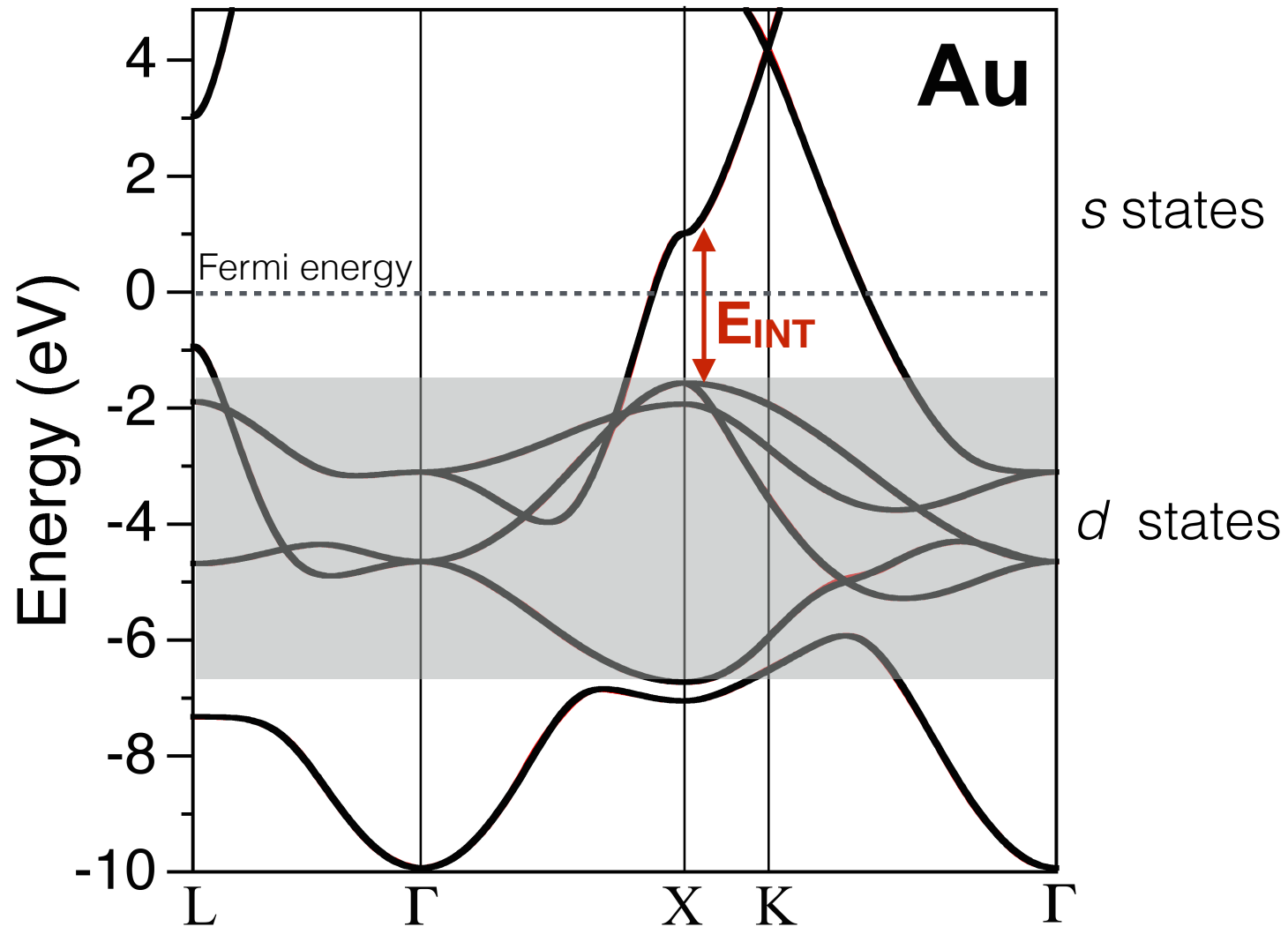
Surface Plasmon Polariton (SPP)-to-Hot Carrier Conversion in Noble Metals



M. Bernardi et al., Nature Communications 6, 7044 (2015)

- 1) Hot carrier generation and energy distribution in Au & Ag
- 2) Ultrafast hot carrier transport – mean free path, relaxation time
- 3) Ideal regime to extract hot carriers

Noble Metals Bandstructure

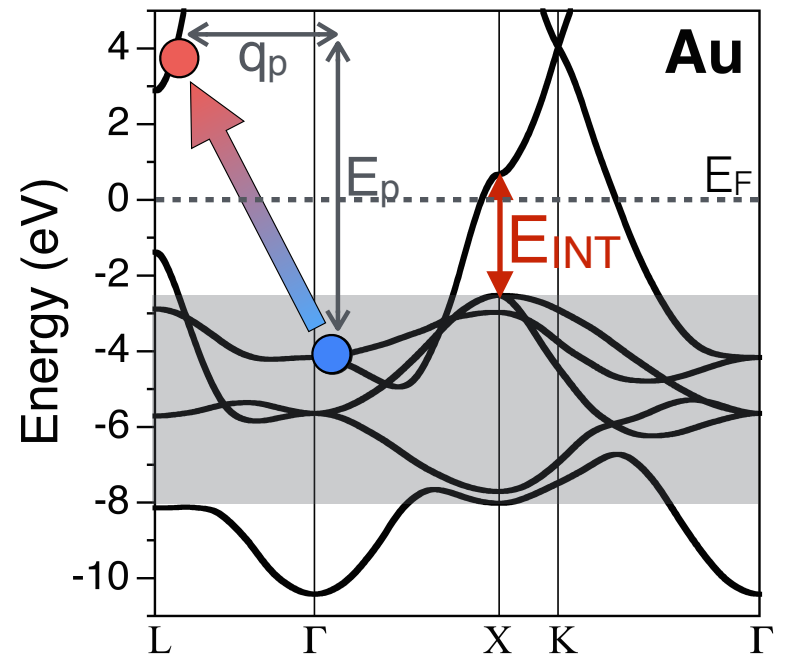
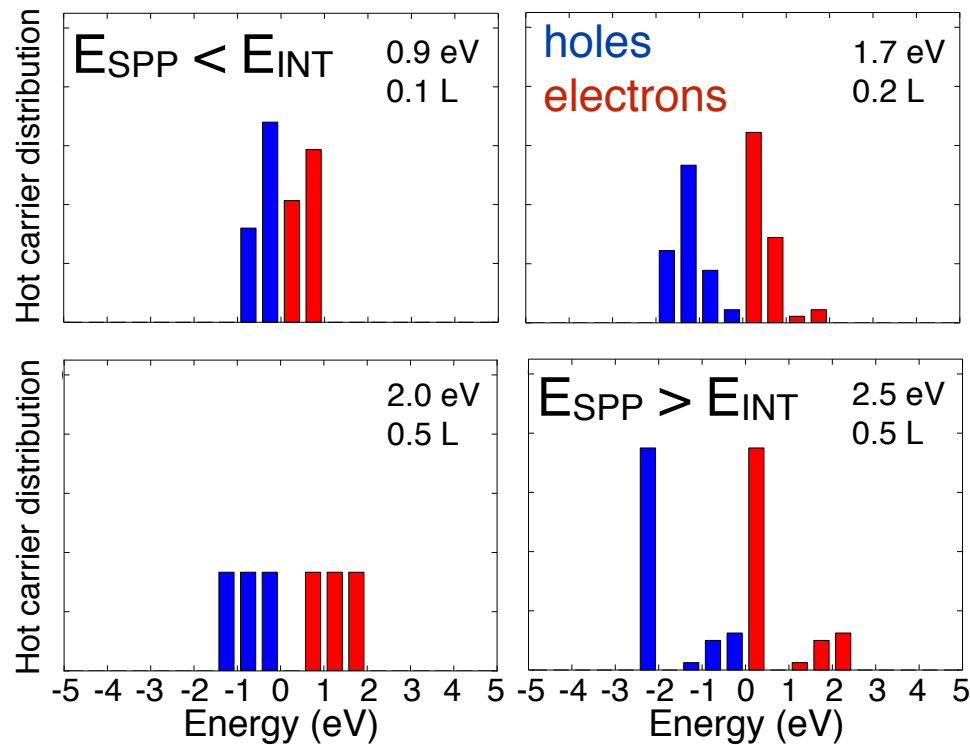


The relative energies of *d* and *s* states are crucial in the generation and transport of hot carriers (need GW)

Hot Carrier Generation

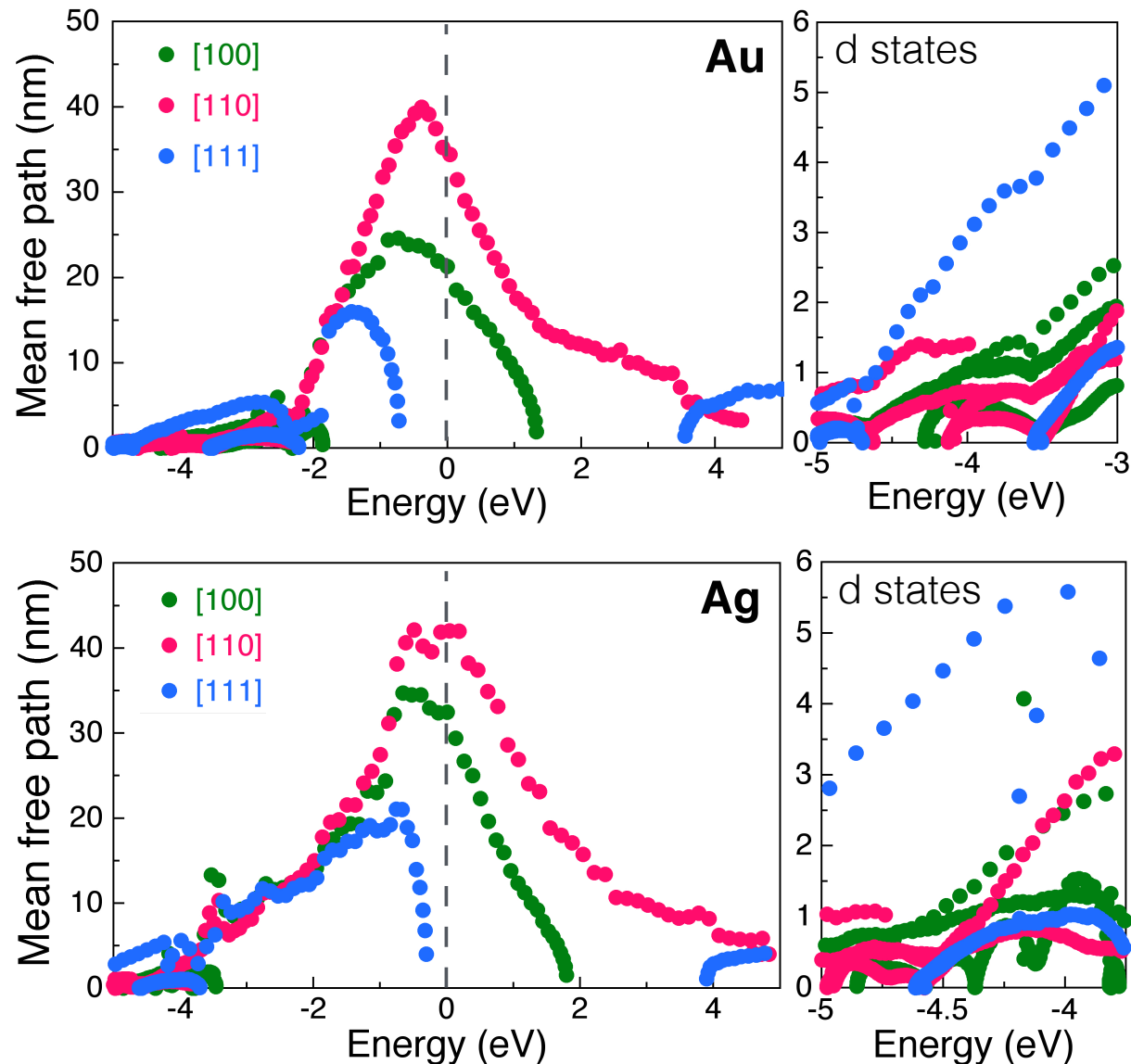
Energy and momentum conserving transitions generate hot carriers with a distribution of energies (in a probabilistic sense)

Hot carrier population distribution (arb. units) vs. Energy



Similar population distributions for Ag

Hot Carrier Mean Free Path

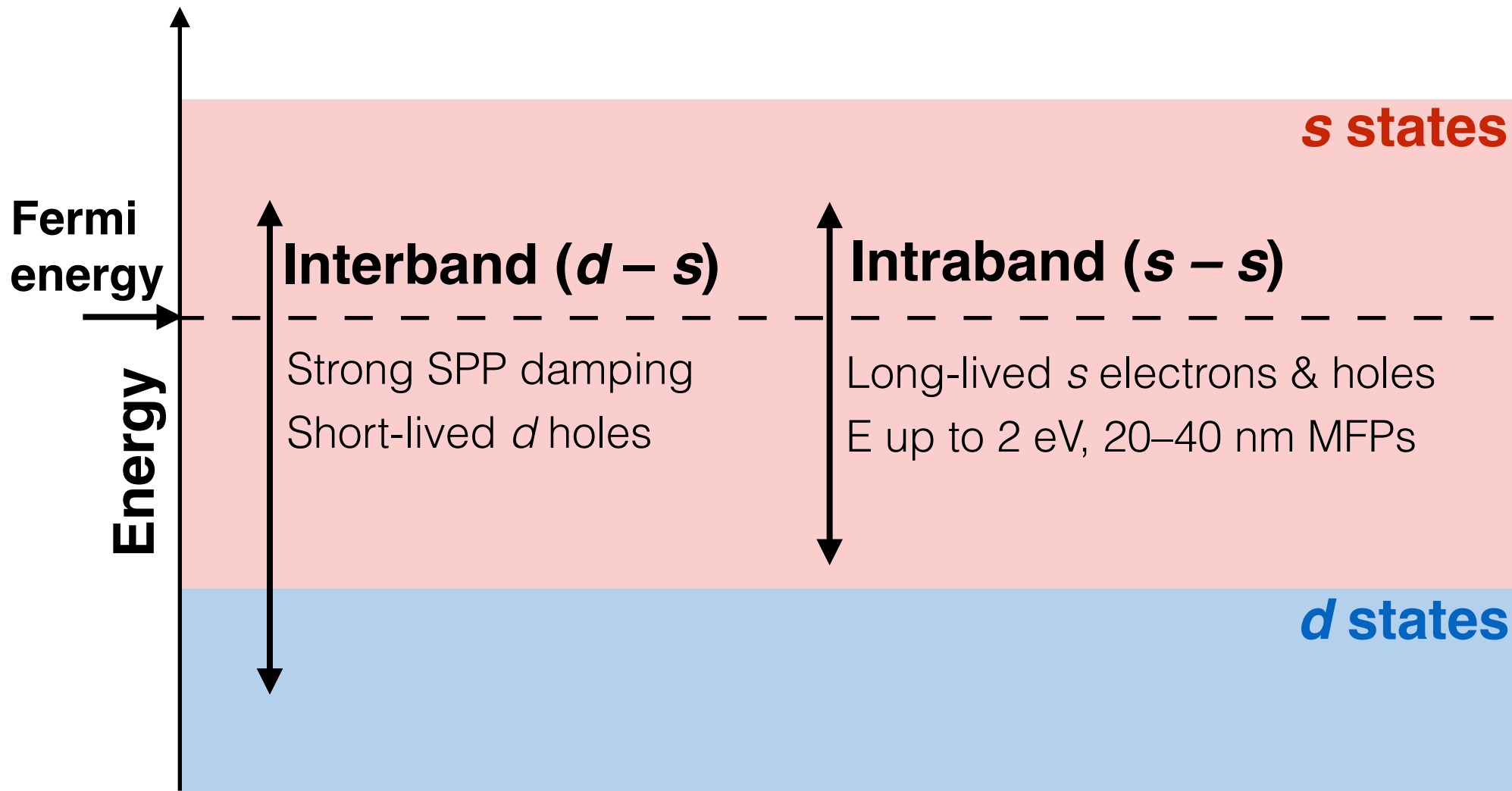


Volcano shape due to strong scattering at $E > 2$ eV away from Fermi energy
s holes ~isotropic, *s* electrons and *d* holes anisotropic, consistent with experiments

Optimization of Hot Carrier Extraction

Two regimes for SPP-to-hot carrier conversion: intraband vs. interband

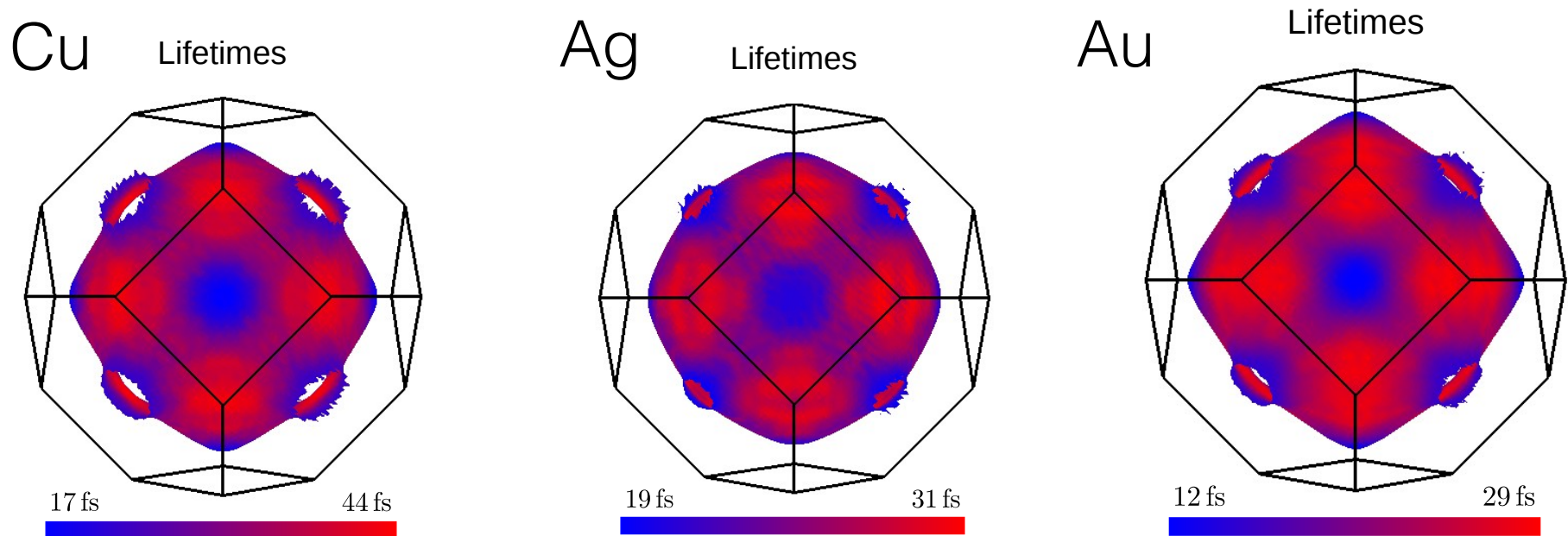
SPP with $E < E_{\text{INT}}$ can be tuned to generate HCs with ~ 2 eV energy & 20-40 nm MFPs



Silver may be better than gold for hot carriers from SPPs

Application to Carrier Transport

“... The conduction electrons are a nuisance in metals” J. M. Ziman, 1964



$$\text{Conductivity } \sigma_{i,j} = e^2 \sum_{n,\mathbf{k}} \tau_{n,\mathbf{k}} v_{n,\mathbf{k},i} v_{n,\mathbf{k},j} \left(-\partial f / \partial E \right)$$

Can predict resistivity within 10% of experiment
Can be applied to metals, semiconductors, insulators

Summary

Carrier dynamics and scattering by electrons and phonons

Design hot carrier devices and experiments

Microscopic understanding of time-resolved experiments

Perturbation theory is promising for excited state timescales

Non-equilibrium theories necessary for coherent / driven dynamics



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