





Improving the performance of ab initio molecular dynamics simulations and band structure calculations for actinide and geochemical systems with new algorithms and new machines

Eric J. Bylaska (PNNL)



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# Outline

## NWChem

- Analyzing EXAFS with ab initio molecular dynamics simulations (AIMD)
- Exact Exchange
  - Brillouin zone integration
  - Fast Localization
- Parallel in time



#### Plane-Wave Density Functional Theory (NWPW module) in NWChem



- Highly scalable
- CG, limited memory BFGS, and RMM-DIIS minimization
- Gamma and Band structure capabilities
- Car-Parrinello (extended Lagrangian dynamics) and Born-Oppenheimer
- Constant energy and constant temperature Car-Parrinello
- Metropolis NVT, NPT
- Fixed atoms in cartesian, SHAKE constraints, translation contraints, and rotation constraints, Metadynamics, TAMD, PMF, equation parser-ecode
- Hamann, Troullier-Martins, and HGH norm-conserving pseudopotentials with optional semicore corrections
  - Interface for CPI and TETER formats
  - Spin-orbit
- PAW (full integration in next release, most functionality already working in development branch)
- FEFF6 integration
- LDA and GGA exchange-correlation potentials (spin-restricted and unrestricted) SIC, pert-OEP, Hartree-Fock and Hybrid Functionals (restricted and unrestricted), DFT+U, Grimme1, Grimme2, Grimme3...complete set of functionals in next release
- Fractional occupation,
- Geometry/unitcell optimization, frequency, transition-state searches, phonon spectra, NEB, String
- AIMD/MM
- Wannier analysis
  - Wavefunction, density, electrostatic, Wannier, density matrix, ELF plotting

#### Molecular simulation of XAFS analysis

#### Objective

 To provide molecular simulation analysis that will support the application of XAFS (XANES) to complex aqueous systems in extreme chemical/ geochemical environments.





### EXAFS and coordination for $UO_2^{2+}(aq)$





 Good EXAFS agreement but recent HEXS experiments suggest a 4-fold state is energetically nearby



### EXAFS and coordination for $UO_2^{2+}(aq)$



- Good EXAFS agreement but recent HEXS experiments suggest a 4-fold state is energetically nearby
- Results from Metadynamics
  - Coordination number collective variable
  - 5-fold state is favored over 4-fold state by  $\Delta A_{5\rightarrow4}$ =0.7 kcal/mol
  - Agrees with  $\Delta G_{expt}$ =1.2 kcal/ mol
  - Predicted associative barrier  $\Delta A_{5 \rightarrow 4}^{\ddagger} \approx 4.7$  kcal/mol
  - Prediction: 6-fold state has short lifetime in solution; not stable relative to 5-fold state.
  - ΔA<sub>5→6</sub>=8 kcal/mol; ΔA<sub>5→6</sub><sup>‡</sup>≈9
     kcal/mol



Illustrates the agreement with data obtained using the full 1<sup>st</sup> principle MD-XAFS method. That is direct simulation of spectra using ab-initio MD. All scattering paths are used. Slide illustrates the contributions from the various scattering paths. The parameter free 1<sup>st</sup> principle simulation will very accurately reproduce both the structural parameters and disorder effects.



The generally excellent agreement of the 1<sup>st</sup> principle MD-XAFS simulation with the data. The scans are calculated by a parameter free method which can be implemented more efficiently than the use of empirical interactions suggesting that this **method can be used to interpret more XAFS spectra in more complex environments**.

## **Second Shell and Defect Structures**



1st principle MD XAFS simulation of Ca<sup>2+,</sup> a relatively weakly interacting ion. Disorder results in no second shell structure.



Scattering for the more structured Zn<sup>2+</sup> ion in the 2nd shell scattering region. Note the difference between the Ca<sup>2+</sup> and Zn<sup>2+</sup> features.

#### Incorporation of incommensurate metals in Iron (oxyhydr)oxides (Ilton, Kerisit)

Strong constraint on thermal disorder Proton dynamics likely important



Determine the solute structure of environmentally important species (e.g., Al<sup>3+</sup>, Mg<sup>2+</sup>, Cl<sup>-</sup>, Fe<sup>3+</sup>) in aqueous solutions as a function of TPX through synergistic simulation and X-ray observation



Old Way – The diagram for the distribution of aluminum species was determined primarily from fitting thermodynamic data using an **assumed speciation scheme**.

- By combining AIMD free energy simulations with XAS spectra can provide a transformative new approach to the development of chemically and thermodynamically highly accurate solution models with exceptional extrapolation properties in TPX.
  - Strategies to search configuration space must be developed.
  - MgCO<sub>3</sub>-H<sub>2</sub>O system
    - Ion pairs in this system control the stability of Mg containing minerals.
  - Nature of ion association of Na<sup>+</sup>(aq) ion with the aluminate ion to form NaAl(OH)<sub>4</sub>(aq) ion pair.



NaAlOH,



#### Calculating exact exchange

#### Algorithm 1: Serial algorithm for calculating exact exchange in a planewave basis

Input:  $\psi - N_g \times N_e$  array Output:  $K\psi - N_g \times N_e$  array for m=1, $N_e$ for n=1,m  $\rho(:) \leftarrow FFT\_rc(\psi(:,m)^*.\psi(:,n)))$   $V(:) \leftarrow FFT\_cr(f_{cutoff}(:)^*.\rho(:))$   $K\psi(:,m) -= V(:)^*.\psi(:,n); if m <> n K\psi(:,n) -= V(:)^*.\psi(:,m)$ end for end for

For Ne=500  $\rightarrow$  500(500+1) = 250,500 three-dimension FFTs per step

For Ng=200x200x200 calculation can readily be run on leadership class machines (e.g. 38640 cores, 4 to each of 9660 processing nodes)

### Simple parallel algorithm for exact exchange



The algorithm is scalable because: →Computation ~Npj^2, →Message passing ~Npj Use replicated space to compute exchange using 3d parallel FFTs along columns (load balanced)

### Exact exchange timings



Basic algorithm works fairly well (80 atoms cell of hematite on Cray XT4 -Franklin system at NERSC) - stalls at 7 seconds by 4096 cpus

- Exchange term is dominant
- Previous algorithm simple to implement
- Requires lots of workspace
- Sends approximately twice as much data as necessary
- Can be improved

### **Exact exchange timings**



Incomplete butterfly algorithm results works fairly well (576 atoms cell of water on Cray XE6 - Hopper system at NERSC)



- Exchange term is dominant
- Previous algorithm simple to implement
- Requires lots of workspace
- Sends approximately twice as much data as necessary

#### Can be improved

- Developed new parallel algorithm for hybrid DFT (Incomplete butterfly) which reduced communication costs by <sup>1</sup>/<sub>2</sub>
- Scaling to at least ~100k
- MP2 algorithm (easily 10<sup>9</sup> 3d FFTs per step)

# Problems with simple implementations of exact exchange – the ugly



#### $E_{x-exact} [\{\psi\}] =$

$$-\frac{1}{2\Omega}\sum_{\sigma=\uparrow\downarrow}\left(\frac{\Omega}{8\pi^{3}}\right)^{2}\int_{BZ}d\mathbf{k}\int_{BZ}d\mathbf{l}\left[\sum_{n=1}^{N_{occ}^{\sigma}}\sum_{m=1}^{N_{occ}^{\sigma}}\sum_{\mathbf{G}}\frac{4\pi}{\left|\mathbf{G}-\mathbf{k}+\mathbf{l}\right|^{2}}\rho_{ml;nk}^{\sigma}(-\mathbf{G})\rho_{nk;ml}^{\sigma}(\mathbf{G})\right]$$

- Integral has singularity at G=0, k=l
- Common (bad strategies?)
  - Set  $4\pi/G^2 \rightarrow 0$
  - Compute dielectric ε for screening?
  - Refine G==0 term by increasing k-points, and using analytic formulas to handle integrals, e.g.

Singular terms – – >

$$-\frac{1}{2\Omega}\sum_{\sigma=\uparrow,\downarrow}\left(\frac{\Omega}{8\pi^{3}}\right)^{2}\rho_{ml;nk}^{\sigma}(-\mathbf{G}=0)\rho_{nk;ml}^{\sigma}(\mathbf{G}=0)\int_{BZ}d\mathbf{k}\int_{BZ}d\mathbf{l}\frac{4\pi}{\left|-\mathbf{k}+\mathbf{l}\right|^{2}}$$

Wannier integration

$$\Rightarrow V_{screened} \left( \mathbf{r} + \mathbf{R} \right) = \frac{1}{|\mathbf{r}|} \text{ for } \left( \mathbf{R} - L/2 \right) \le \mathbf{r} + \mathbf{R} \le \left( \mathbf{R} + L/2 \right)$$

Results for Be atom(s)





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# Another (Derivation?) Justification for 1/r Kernel



# If there is no Brillioun zone dependency in the overlap densities then

$$E_{x-exact}[\{\psi\}] - - >$$

$$-\frac{1}{2\Omega} \sum_{\sigma=\uparrow,\downarrow} \left[ \sum_{n=1}^{N_{occ}^{\sigma}} \sum_{m=1}^{N_{occ}^{\sigma}} \sum_{\mathbf{G}} \left[ \left(\frac{\Omega}{8\pi^{3}}\right)^{2} \int_{BZ} d\mathbf{k} \int_{BZ} d\mathbf{l} \frac{4\pi}{|\mathbf{G}-\mathbf{k}+\mathbf{l}|^{2}} \right] \right]$$

Thus the screened potential is

$$V_{\text{ScreenedCoulomb}}[\mathbf{G}] = \left(\frac{\Omega}{8\pi^3}\right)^2 \int_{BZ} d\mathbf{k} \int_{BZ} d\mathbf{l} \frac{4\pi}{\left|\mathbf{G} - \mathbf{k} + \mathbf{l}\right|^2}$$



#### Evaluation of Exchange for $\Gamma$ Calculation





## Localization Algorithm of Damle, Lin, and Ying MSL

# **Plotting** $\rho(\mathbf{r},\mathbf{r}'=\mathbf{r}_i) \quad i=\Pi_{1,Ne}$



### The density matrix is

- Severely rank deficient, i.e. a density matrix for Ne orbitals has a rank=Ne
- Localized (real-space) orbitals by selecting certain columns(or r')
- In principle just Ne columns are needed to regenerate the density matrix
- Currently testing algorithm on HPC systems

$$\rho(\mathbf{r},\mathbf{r}') = \rho(\mathbf{r},\mathbf{r}'=\mathbf{r}_1\cdots\mathbf{r}_{Ne})\left[\rho(\mathbf{r}_i,\mathbf{r}_j)\right]^{-1}\rho(\mathbf{r}=\mathbf{r}_1\cdots\mathbf{r}_{Ne},\mathbf{r}')$$

#### AIMD and MD Still Need Faster Time To Solutions: The Irrational Pursuit Of Solving The Schrödinger Equation In less than a Second Per Step

- Current ab-initio molecular dynamics simulations for 10 to 100 picoseconds can take several months to complete
- The step length in ab initio molecular dynamics simulation is on the order of 0.1...0.2 fs/step

  - 20 ps of simulation time → 200,000 steps

     At 1 second per step → 2-3 days
     At 10 seconds per step → 23 days
     At 30 seconds per step → 70 days

 $HCI+4H_2O$ MP2/6-311++G(2d, 2p) force evaluation takes 32 seconds!

- 1 ns of simulation time → 10,000,000 steps

   at 1 second per step → 115 days of computing time
   At 10 seconds per step → 3 years
   At 30 seconds per step → 9 years

- At 0.1 seconds per step  $\rightarrow$  11.5 days

- For classical molecular dynamics, time step  $\sim$ = 1fs/step

  - 1µs of simulation time → 1,000,000,000 steps

     1 millisecond per step → 11.6 days of computing time
     1 second per step → 31 years of computing time
     10 seconds per step → 310 years of computing time

    - $-1 \mu s$  per step  $\rightarrow 16.6$  minutes

#### **Parallel in Time**



- Increasing the time step ( $\Delta$ t) in time integration quickly becomes unstable
- One approach to bridging these temporal scales is the development of algorithms which parallelize over time, i.e. parallel in time algorithms
- The central philosophy of parallel in time integration is to start with a guess for the trajectory over some fixed time interval and then attempt to relax it until it approximates the "true" trajectory.



#### New Parallel In Time Algorithms Without Using Approximate Models (W/ J.Q. Weare): Fixed Point Parallel in Time Algorithms

These algorithms transform standard forward substitution time integration solvers, i.e.  $x_{i+1} \leftarrow f(x_i)$ , into fixed-point root problems

$$\mathbf{F}(\mathbf{X}) = \mathbf{0} \quad \text{or} \quad \begin{pmatrix} x_1 - f(x_0) \\ x_2 - f(x_1) \\ \vdots \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ \vdots \end{pmatrix}$$

Can be solved using a variety of optimization techniques, including preconditioned fixed-point, quasi-Newton, and preconditioned quasi-Newton optimization methods. These algorithms can be parallelized since the evaluation of the trial root function F(X) can be done in parallel.



#### **Parallel in Time: Fixed Point Iteration**



The serial solution to time integration,

with initial condition

is 
$$X_{trajectory} = \begin{bmatrix} f(x_0) \\ f(f(x_0)) \\ f(f(f(x_0))) \\ f(f(f(x_0))) \\ f(f(f(f(x_0)))) \end{bmatrix}$$

 $x_{i+1} = f(x_i)$ 

Using column vector to store each step in the time iteration from i=1,4

This equation can also be solved by a fixed point iteration over the whole path or trajectory

 $x_{0} = x_{0}$ 

$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$
 or

Parallelized by distributing work over rows

$$\begin{bmatrix} x_{1}^{(k+1)} \\ x_{2}^{(k+1)} \\ x_{3}^{(k+1)} \\ x_{4}^{(k+1)} \end{bmatrix} = \begin{bmatrix} x_{1}^{(k)} \\ x_{2}^{(k)} \\ x_{3}^{(k)} \\ x_{4}^{(k)} \end{bmatrix} - \begin{bmatrix} x_{1}^{(k)} - f(x_{0}) \\ x_{2}^{(k)} - f(x_{1}^{(k)}) \\ x_{3}^{(k)} - f(x_{2}^{(k)}) \\ x_{4}^{(k)} - f(x_{3}^{(k)}) \end{bmatrix}$$



Solving 
$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$

**Guess the Initial Path** 

$$X^{(1)} = \begin{bmatrix} b \\ c \\ d \\ e \end{bmatrix}$$



Solving 
$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$

$$\begin{bmatrix} f(x_0) \\ f(b) \\ f(c) \\ f(d) \end{bmatrix} = \begin{bmatrix} b \\ c \\ d \\ e \end{bmatrix} - \begin{bmatrix} b - f(x_0) \\ c - f(b) \\ d - f(c) \\ e - f(d) \end{bmatrix}$$

Each step of this global iteration can be parallelized by evaluating each row on a different cpu



Solving 
$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$
  
k=2

$$\begin{bmatrix} f(x_0) \\ f(f(x_0)) \\ f(f(b)) \\ f(f(c)) \end{bmatrix} = \begin{bmatrix} f(x_0) \\ f(b) \\ f(c) \\ f(d) \end{bmatrix} - \begin{bmatrix} f(x_0) - f(x_0) \\ f(b) - f(f(x_0)) \\ f(b) - f(f(x_0)) \\ f(c) - f(f(b)) \\ f(d) - f(f(c)) \end{bmatrix}$$

Each step of this global iteration can be parallelized by evaluating each row on a different cpu



Solving 
$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$

**k=3** 

$$\begin{bmatrix} f(x_0) \\ f(f(x_0)) \\ f(f(f(x_0))) \\ f(f(f(x_0))) \\ f(f(f(b))) \end{bmatrix} = \begin{bmatrix} f(x_0) \\ f(f(b)) \\ f(f(c)) \end{bmatrix} - \begin{bmatrix} f(x_0) - f(x_0) \\ f(f(x_0)) - f(f(x_0)) \\ f(f(b)) - f(f(x_0))) \\ f(f(c)) - f(f(f(b))) \end{bmatrix}$$

Each step of this global iteration can be parallelized by evaluating each row on a different cpu



Solving 
$$X^{(k+1)} = X^{(k)} - F(X^{(k)})$$



# $\begin{cases} f(x_0) \\ f(f(x_0)) \\ f(f(f(x_0))) \\ f(f(f(x_0))) \\ f(f(f(x_0))) \\ f(f(f(x_0))) - f(f(f(x_0))) \\ f(f(f(f(x_0))) - f(f(f(x_0)))) \\ f(f(f(f(b))) - f(f(f(f(x_0)))) \\ f(f(f(f(x_0)))) \\ f(f(f(f(x_0))) \\ f(f(f(x_0))) \\ f(f(x_0)) \\ f($ $f(x_0)$ $f(f(x_0))$ $f(f(f(x_0)))$ $f(f(f(f(x_0))))$

Exact solution in 4 steps, but no speedup!

#### Improving Fixed Point Parallel in Time Algorithm

- For speedup to occur the root finding iterations needs to converge in less than M iterations, where M is the path length!
- Our strategy is to use a variety of optimization techniques, including preconditioned fixed-point, quasi-Newton, and preconditioned quasi-Newton optimization methods to obtain speedup
- Currently working on FAS methods Fixed Point

Quasi-Newton



#### Real Example: 1000 atom Stillinger-Weber MD Simulation

Path error for each sweep of a quasi-Newton parallel in time algorithm

- The maximum ideal speedup (M/K) observed was 8.7 for M=96 and timestep=5.0, and N<sub>cpu</sub>=M=96
- A true speedup of 5.2 was be obtained by parallelizing over time alone.



# Real Example: HCI+4H<sub>2</sub>O MP2 AIMD Simulations

- True speedup of 8.9 seen by parallelizing over time alone
- Energy conservation maintained





- Parallelization can also be done over forces and time. For a MP2/6-311++G(2d,2p)
  - ▶ Parallelizing over force alone  $\rightarrow$  32 seconds per step
    - 16 cpus  $\rightarrow$  93 seconds per step
    - ◆ 32 cpus  $\rightarrow$  54 seconds per step
    - ♦ 64 cpus  $\rightarrow$  32 seconds per step
  - ▶ Paralleling forces and time  $\rightarrow$  6.9 seconds per step
    - ◆  $16x40 \text{ cpus} = 640 \text{ cpus} \rightarrow 16 \text{ seconds per step}$
    - ◆ 32x40 cpus = 1280 cpus → 11 seconds per step
    - $64x40 \text{ cpus} = 2560 \text{ cpus} \rightarrow 6.9 \text{ seconds per step}$

#### Useful Across Slow Networks: From Hawaii To Chicago/ San Diego And Back In Less Than 5 Seconds







- Significant progress has been made in terms of accuracy, efficiency, and scalability of AIMD methods in recent years.
  - Demonstrated that it can be used to interpret EXAFS experiments
  - Hybrid-DFT, higher-levels methods, and Free energy methods now feasible for many systems
- New localization algorithms show promise for speeding up exact exchange calculations
- Parallel in time algorithms show promise in quantum chemistry and molecular dynamics
  - Newly developed quasi-Newton parallel in time algorithms are able to give factor of ~10 speedups, even without preconditioning
  - Suitable for cloud computing

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PNNL extreme scale LDRD for support for parallel implementations.

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