

Electronic Structure 2018

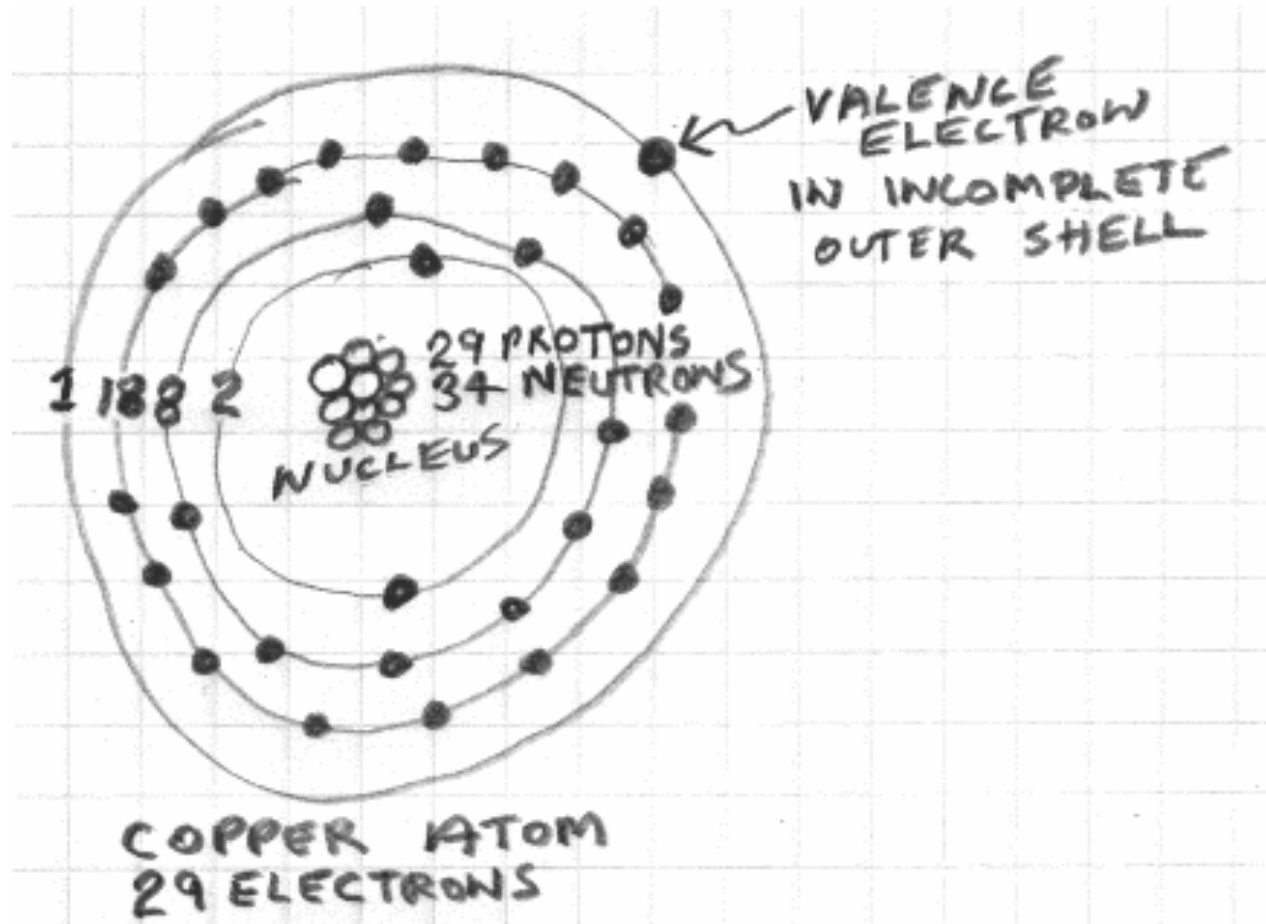
---

# *Interaction Physics in Semimetals*

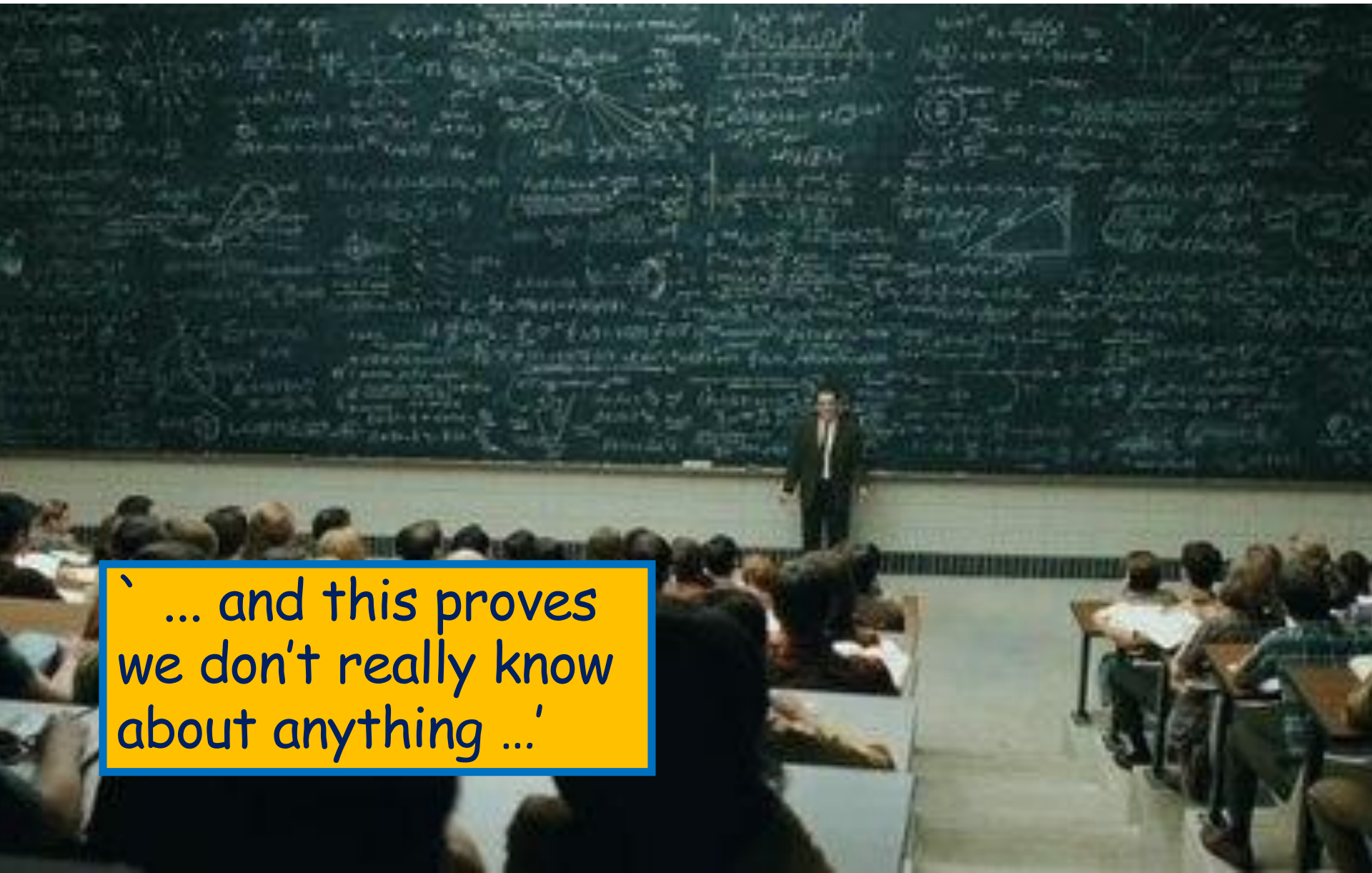
Fei Xue Fengcheng Wu Juanjo Palacios  
AHM - UT Austin



# The Standard Model of Chemistry

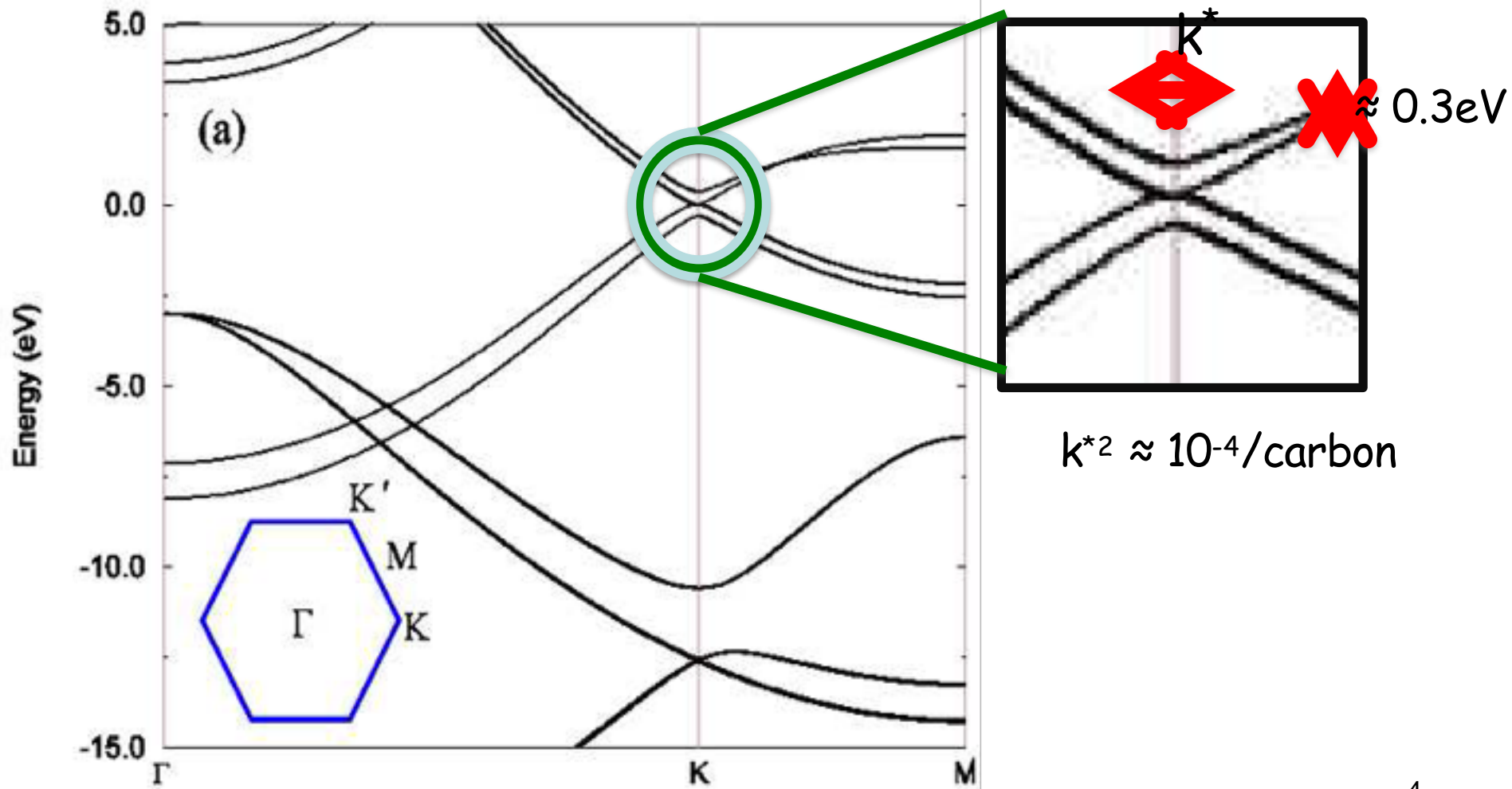


# Many-Electron Quantum Mechanics

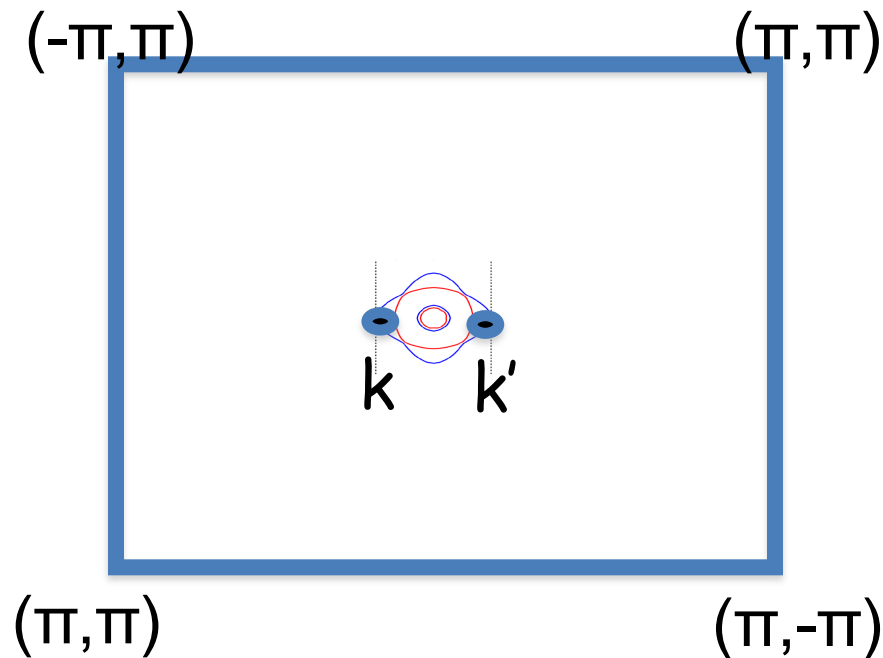


` ... and this proves we don't really know about anything ...'

# Electronic Structure of Bilayer Graphene



# Coulomb Interactions and Continuum Models



$$\langle k' | V_{ee} | k \rangle \sim \sum_{|R| < k_F^{-1}} \frac{e^2}{R} e^{i(k-k') \cdot R}$$



1924-2018

David Pines

Random Phase  
Approximation

# 2D Topological Insulators

## BHZ Model

Decoupled  
Time-Reversed  
Partners

$$\hat{H} = \sum_{\vec{k}} \psi_{\vec{k}}^\dagger \begin{pmatrix} H_{0,\uparrow} & 0 \\ 0 & H_{0,\downarrow} \end{pmatrix} \psi_{\vec{k}}$$

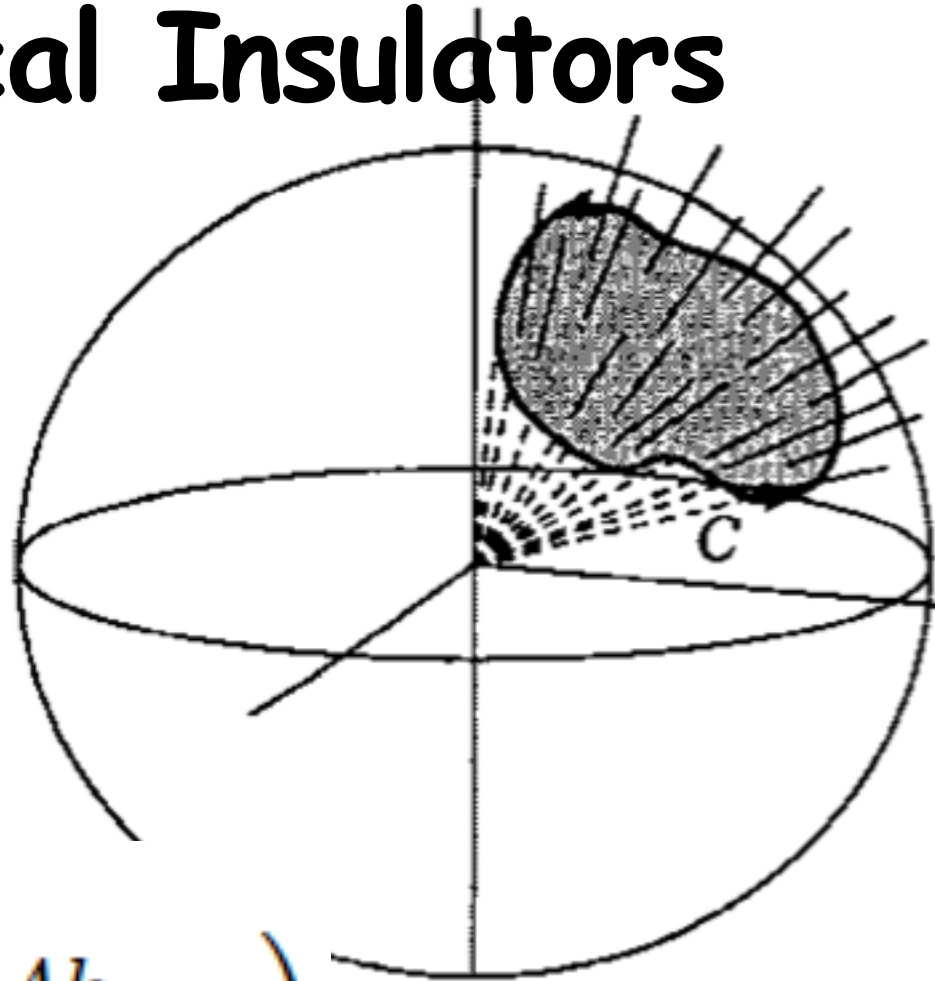
$S_z = 1/2$

$$H_{0,\downarrow} = \begin{pmatrix} \frac{\hbar^2 k^2}{2m_e} + E_c & -Ak_- \\ -Ak_+ & -\frac{\hbar^2 k^2}{2m_h} + E_v \end{pmatrix}$$

$J_z = 3/2$

# 2D Topological Insulators

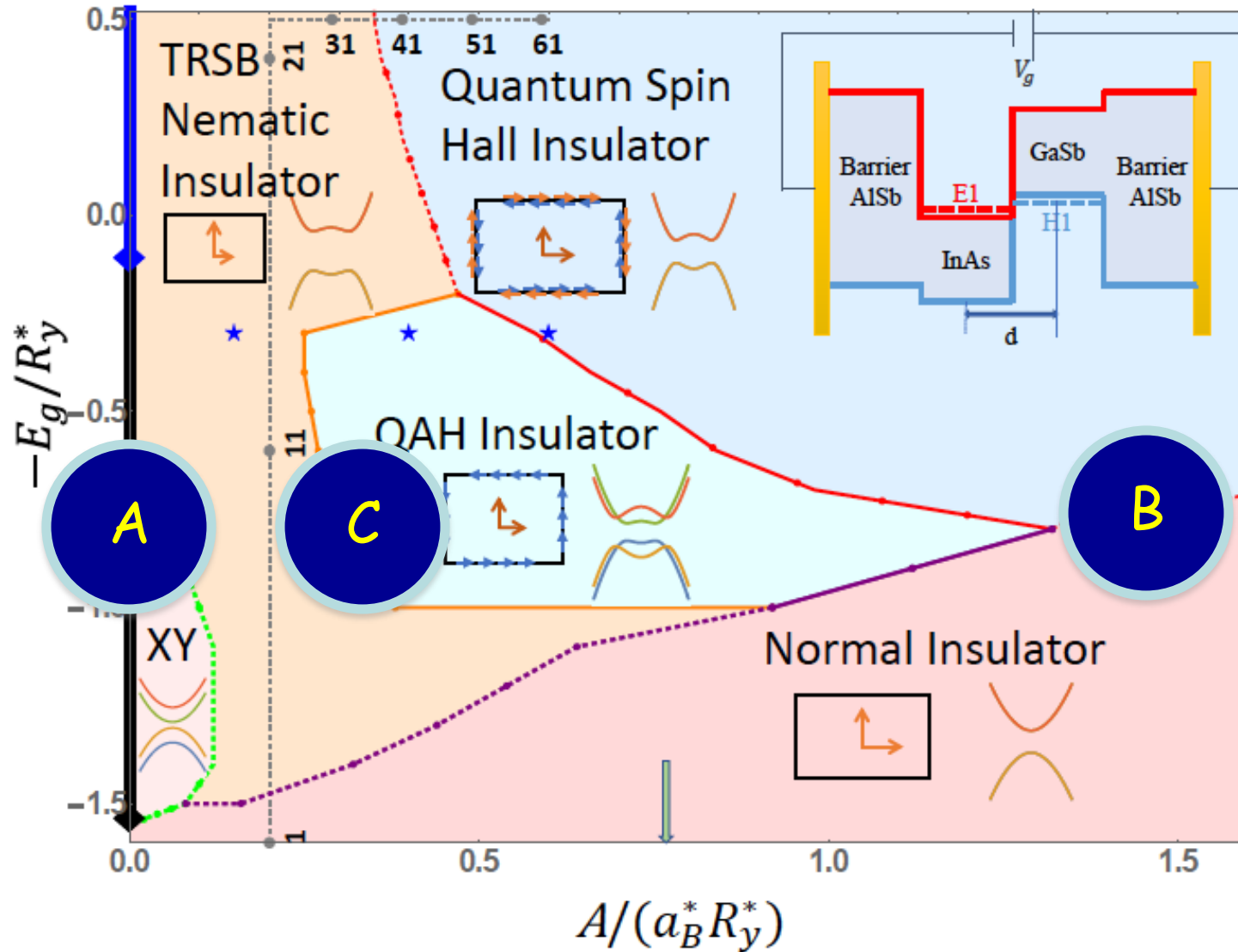
BHZ Model

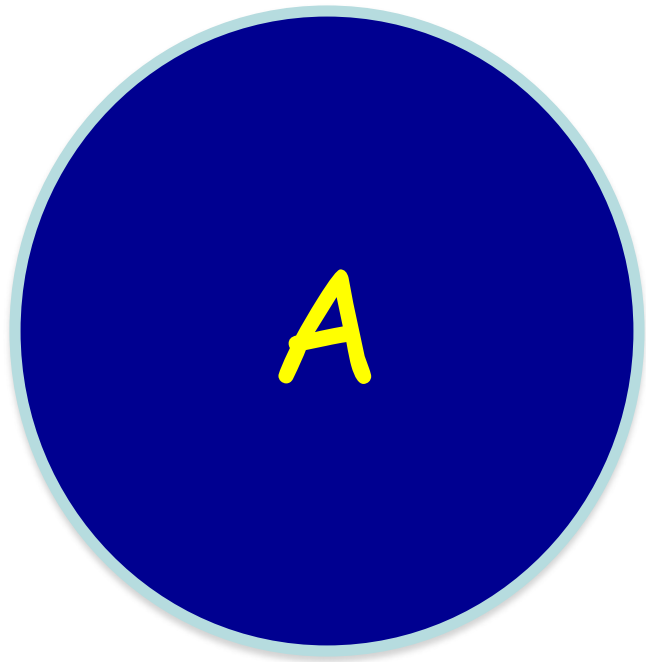


$$H_{0,\downarrow} = \begin{pmatrix} \frac{\hbar^2 k^2}{2m_e} + E_c & -Ak_- \\ -Ak_+ & -\frac{\hbar^2 k^2}{2m_h} + E_v \end{pmatrix}$$



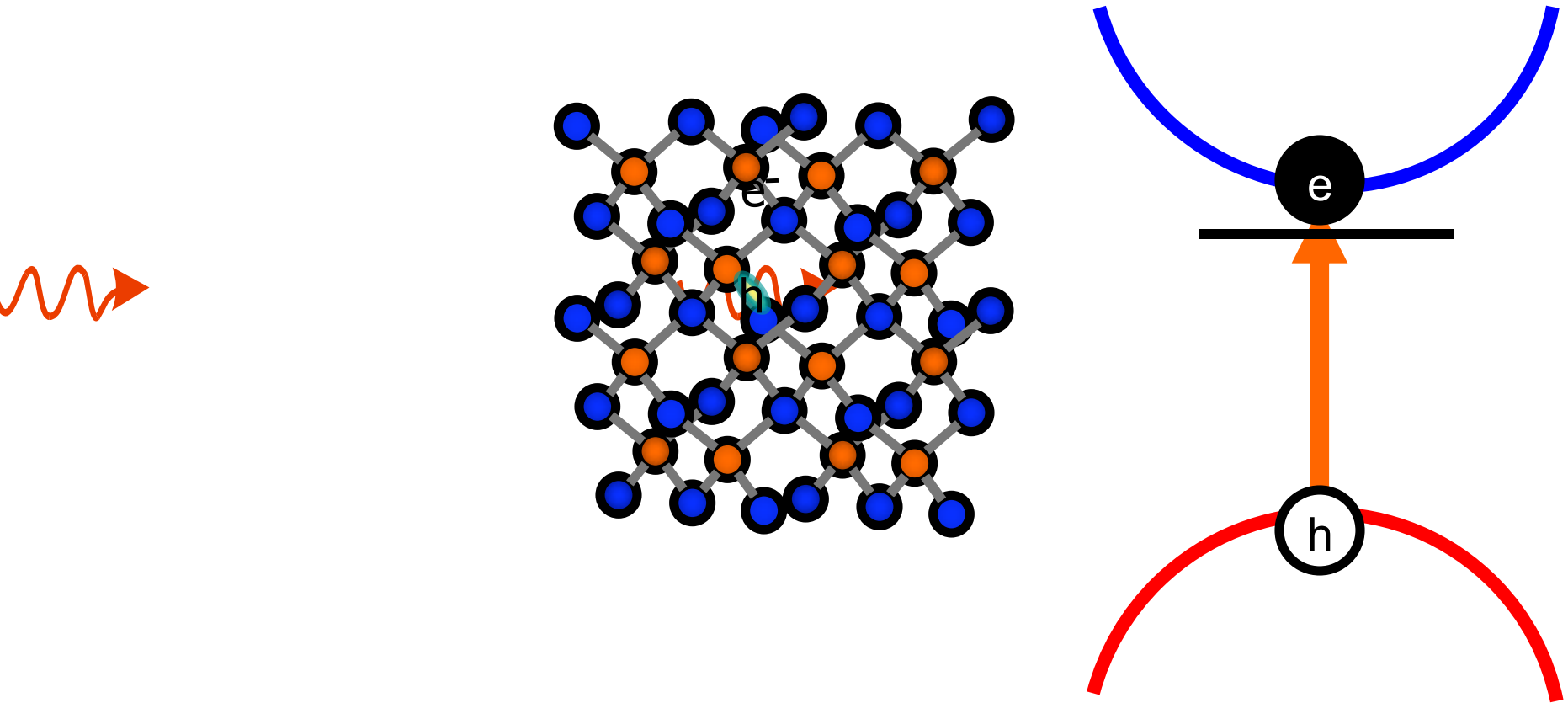
Xue & AHM, arXiv:1710.00410 PRL (2018)





# Exciton Superfluids

# Excitons - Elementary Excitations of Intrinsic Semiconductors



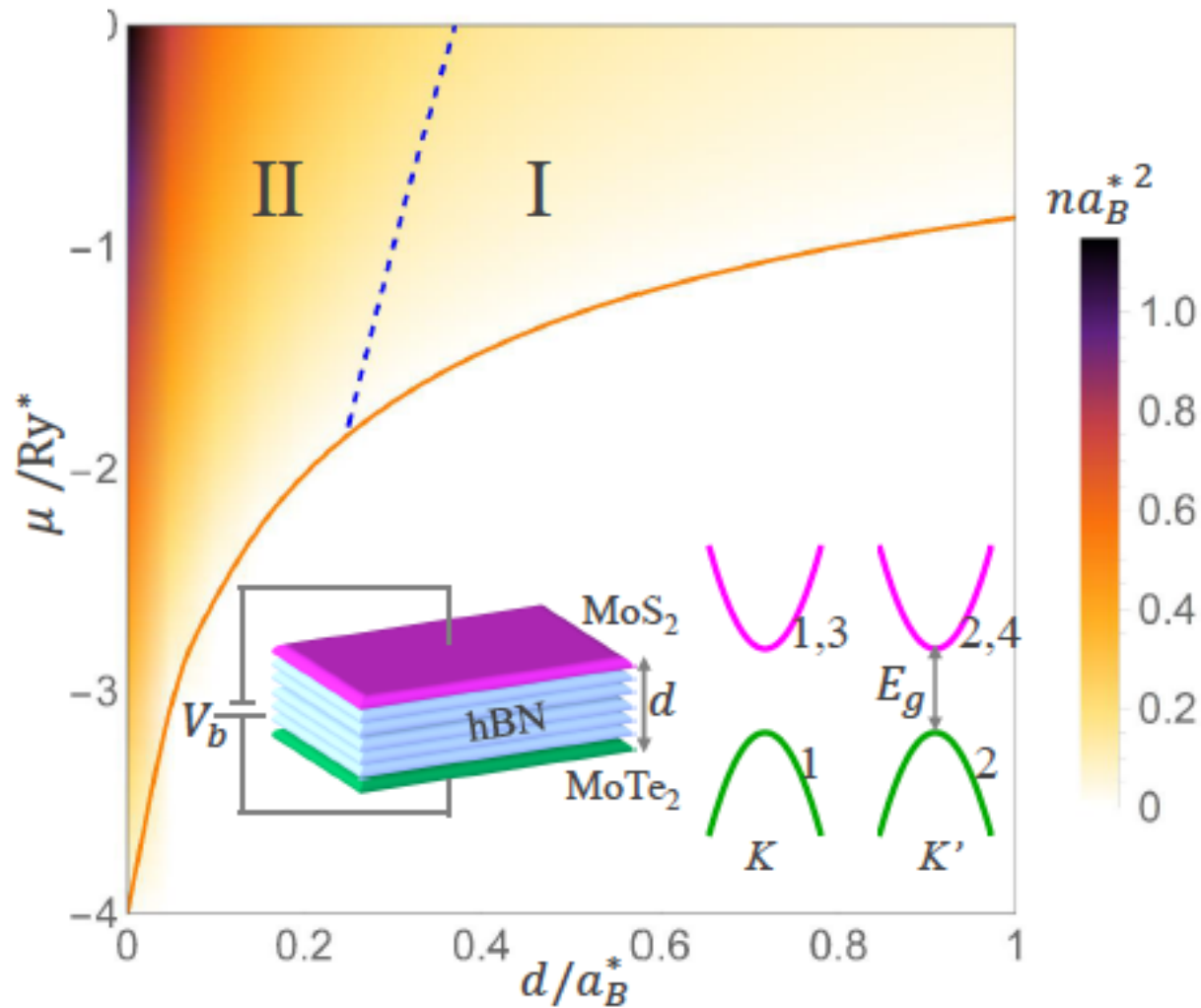
# Bose-Einstein Condensation

Einstein 1925

$$n = \frac{(2\pi m k T)^{\frac{3}{2}} V}{h^3} \sum_{l=1}^{\infty} \tau^{-\frac{3}{2}} \dots (24)$$

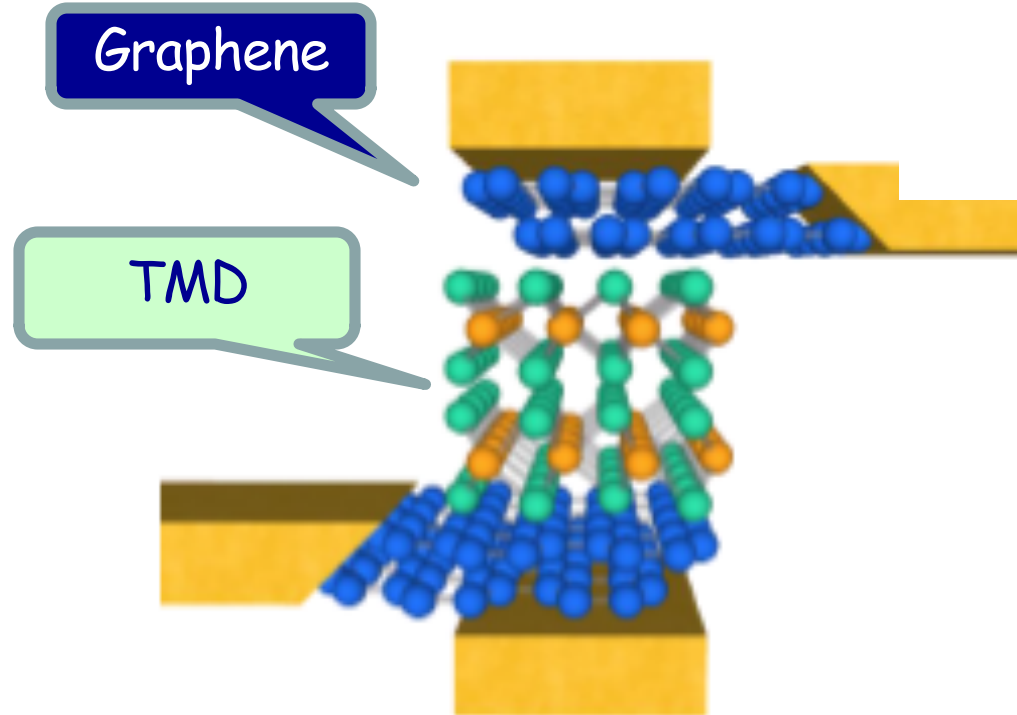
University of Leiden  
Einstein Archive

# TMD Bilayer XC Phase Diagram



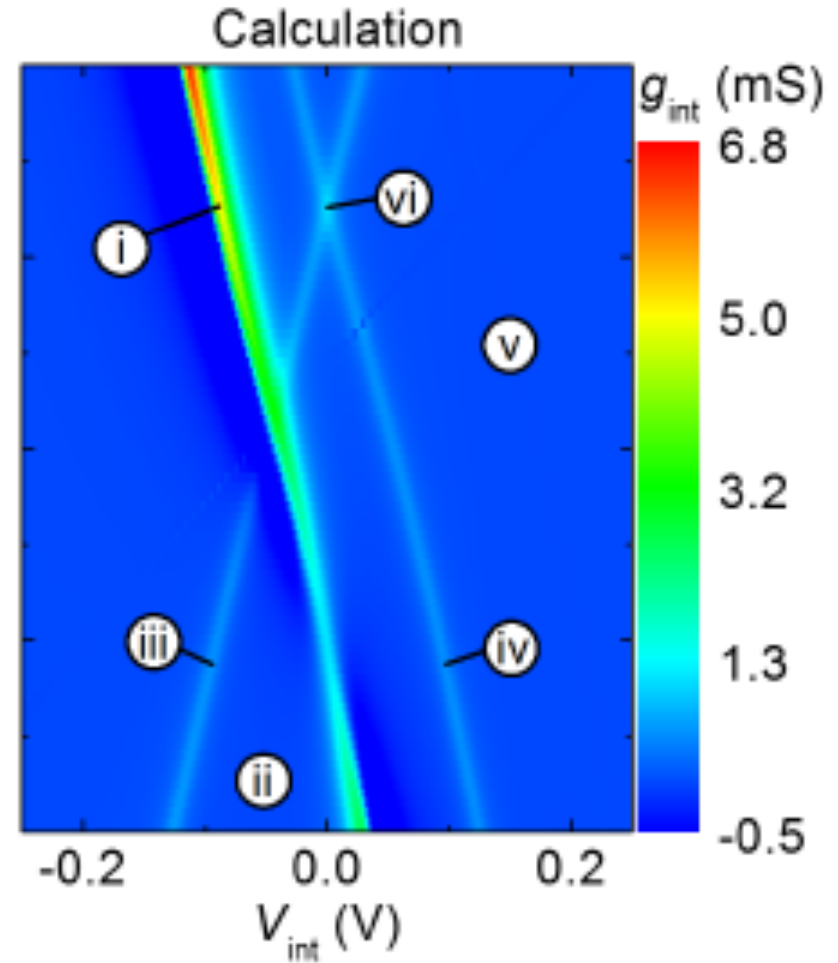
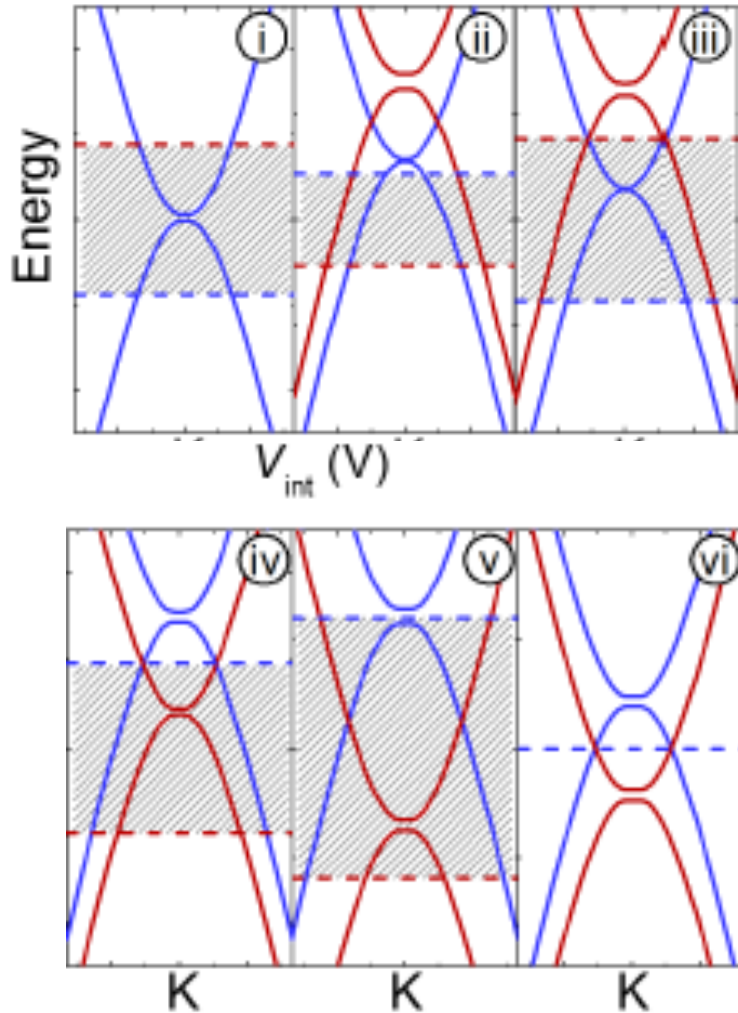
Wu & AHM PRB (2015)

# TMD Bilayer XC Phase Diagram



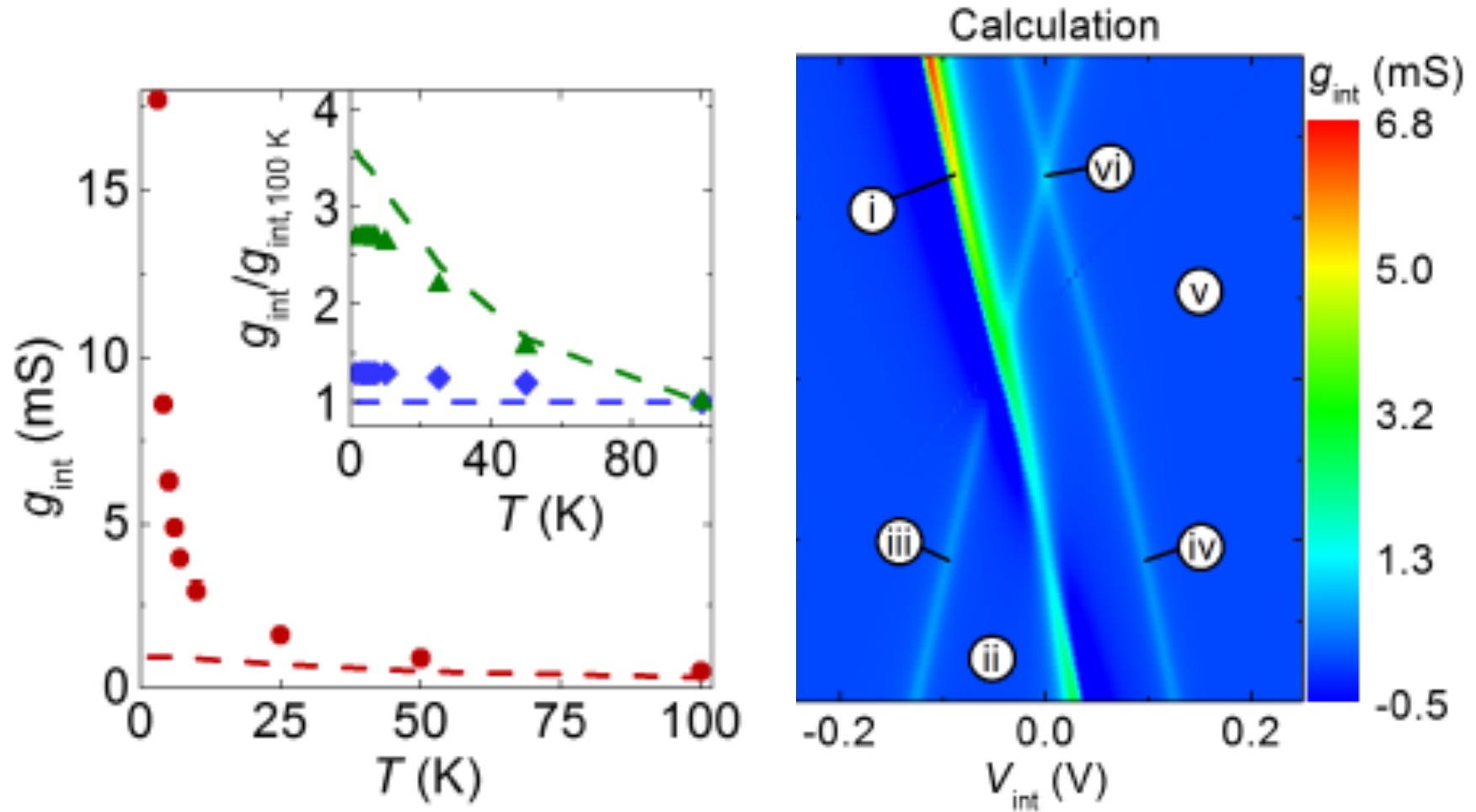
Burg et al. arXiv:1802.07331 - PRL (2018)

# TMD Bilayer XC Phase Diagram



Burg et al. arXiv:1802.07331 - PRL - to appear

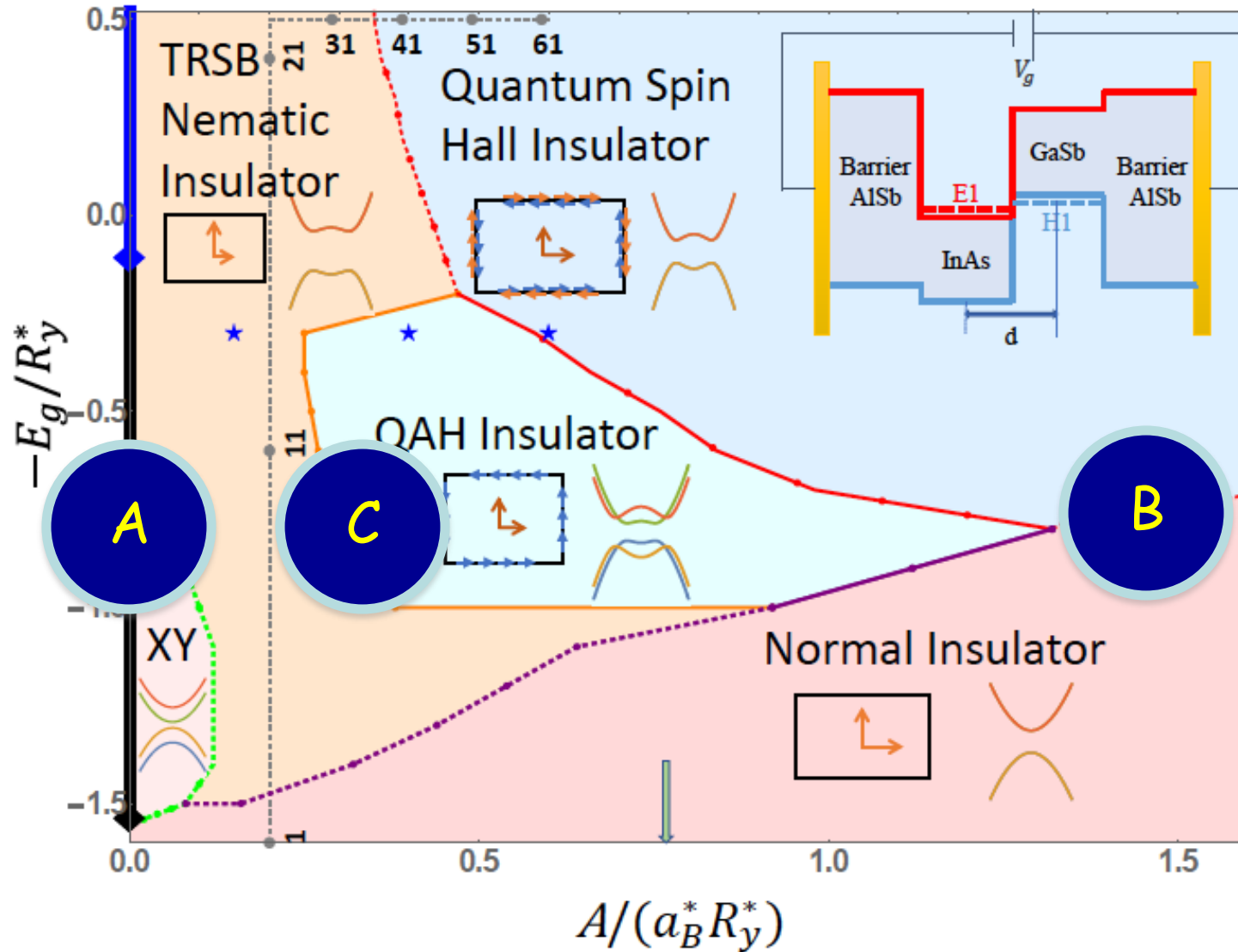
# TMD Bilayer XC Phase Diagram



Burg et al. arXiv:1802.07331 - PRL (2018)



Xue & AHM, arXiv:1710.00410 PRL (2018)

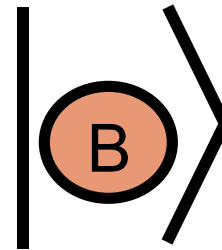
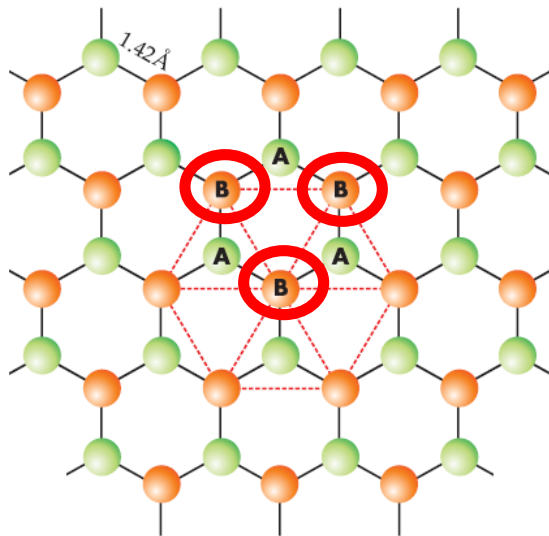
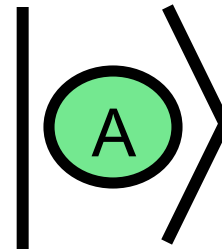
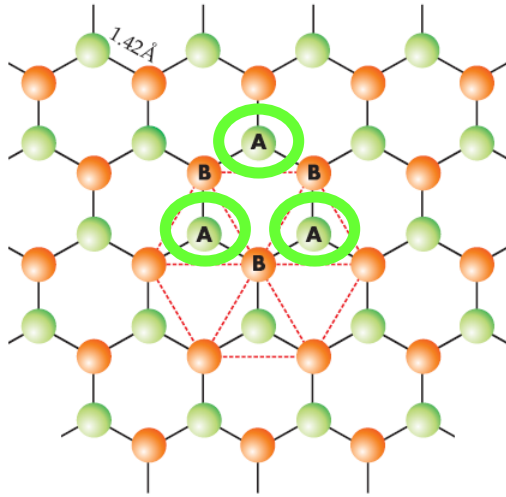


# Quantum Anomalous Hall Effect

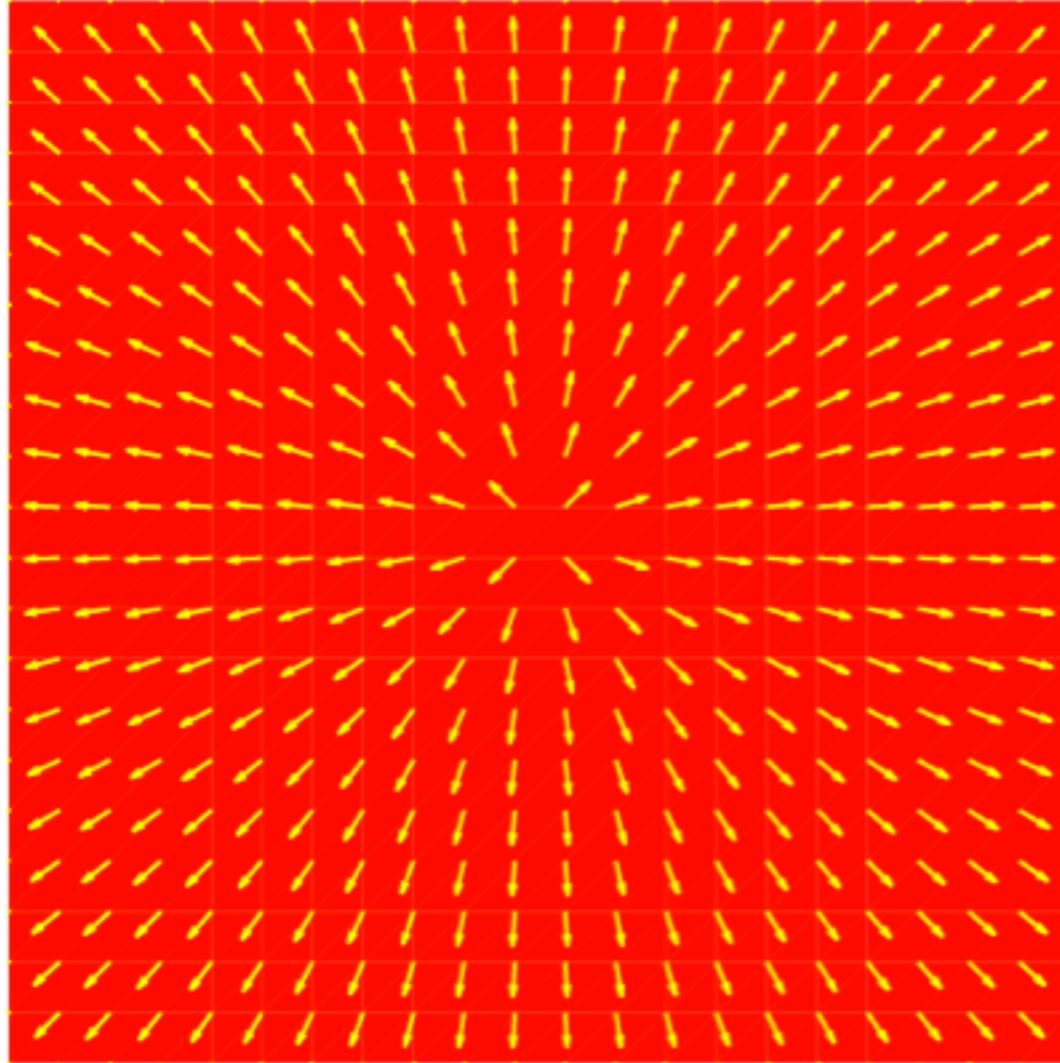


B

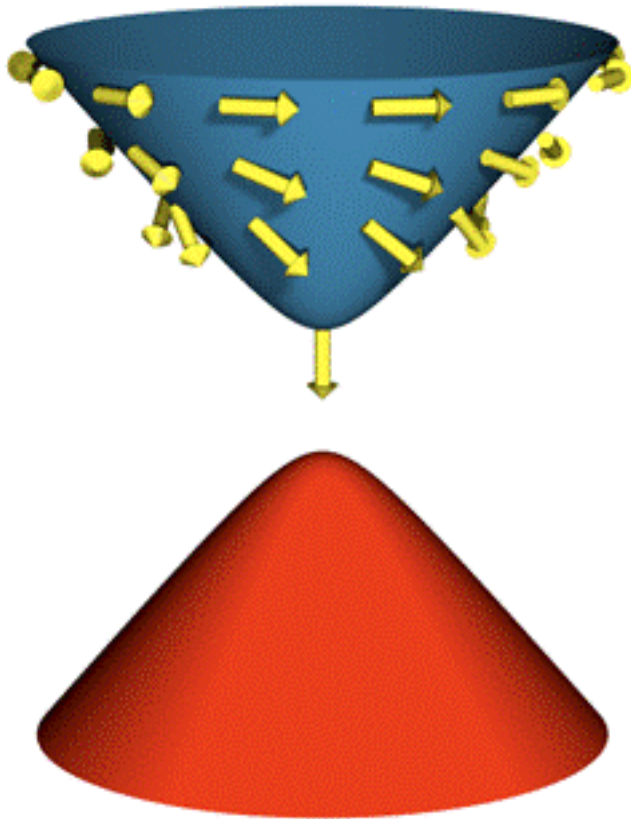
# Sublattice-Pseudospins



# Band Eigenstate Pseudospins



# Band Eigenstate Pseudospins



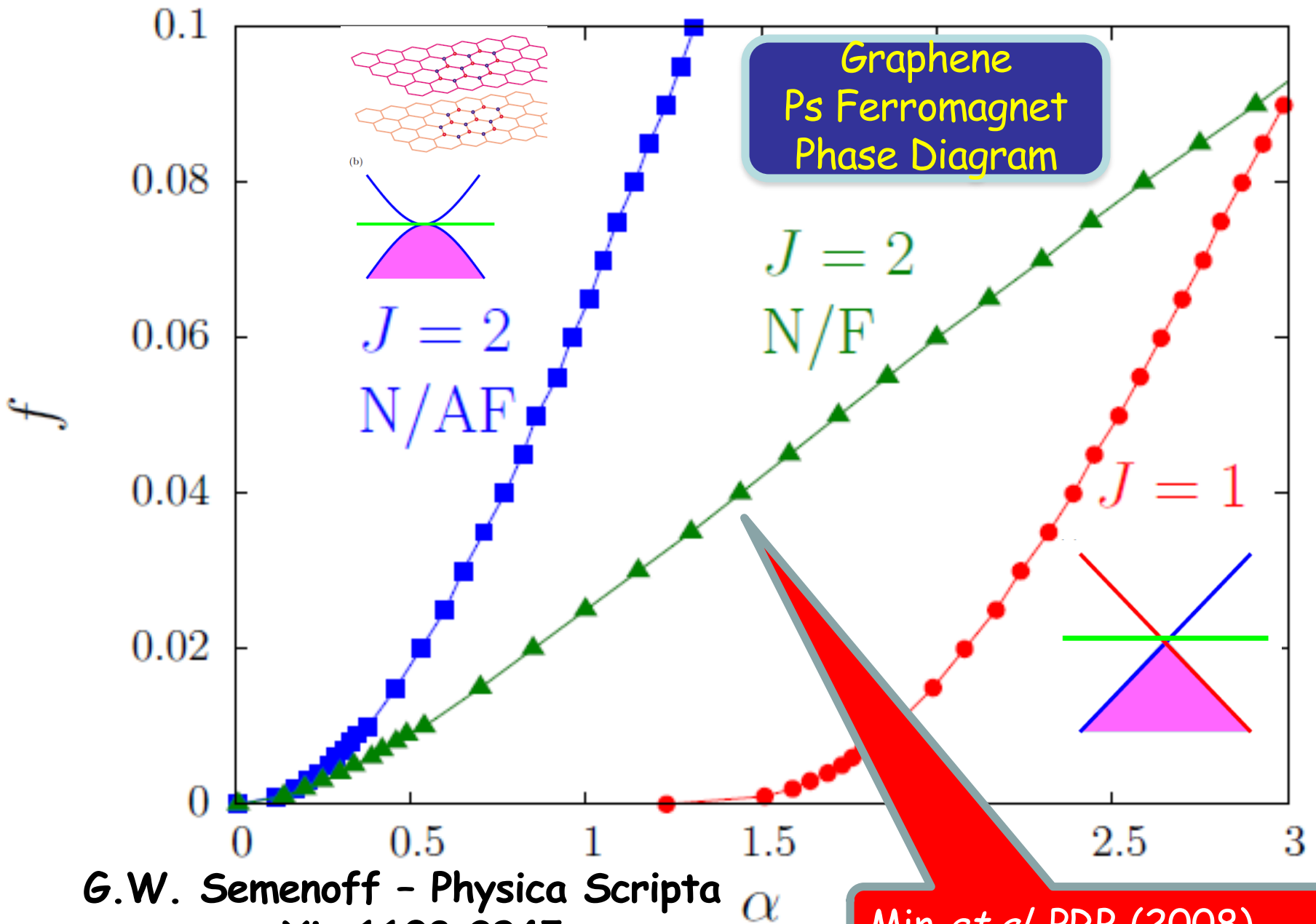
$$\mathcal{H} = \beta mc^2 + \hbar c \vec{\alpha} \cdot \vec{k}$$

Massive Dirac Equation - 3D

Sublattice Staggered  
Potential

$$\mathcal{H} = \tau_z mv^2 + \hbar v \vec{\tau} \cdot \vec{k}$$

Massive Dirac Equation - 2D

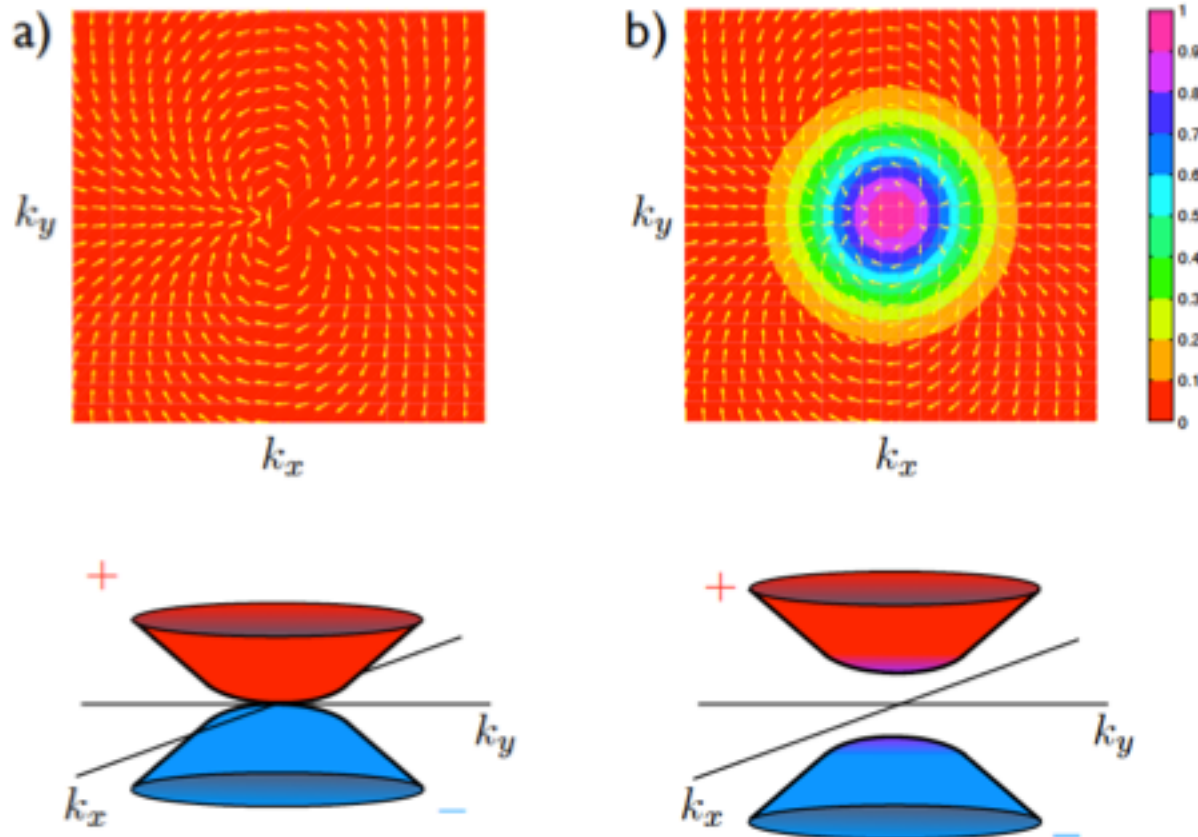


G.W. Semenoff - Physica Scripta  
arXiv:1108.2945

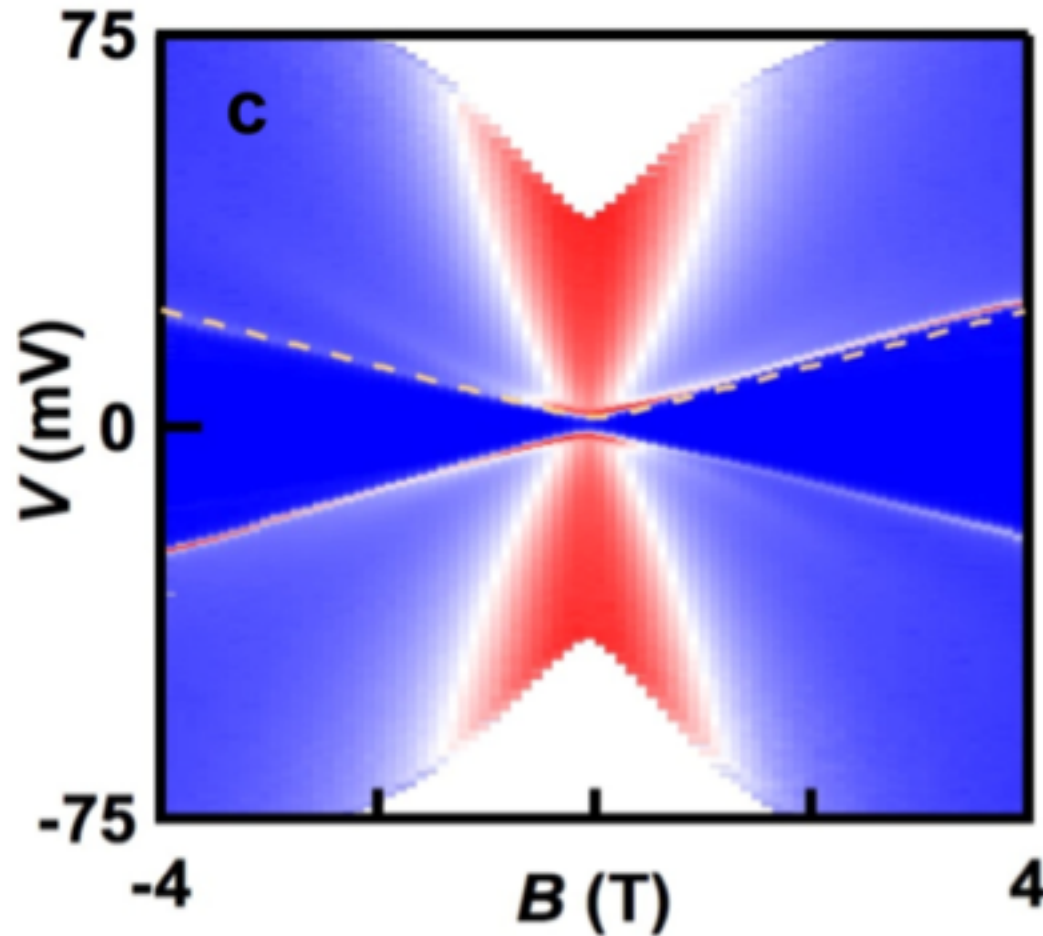
Min et al. PRB (2008)

# Momentum Space Vortex Core

- $\delta n \approx 10^{-5}/C$
- $\Delta \approx 10^{-2} \text{ eV}$



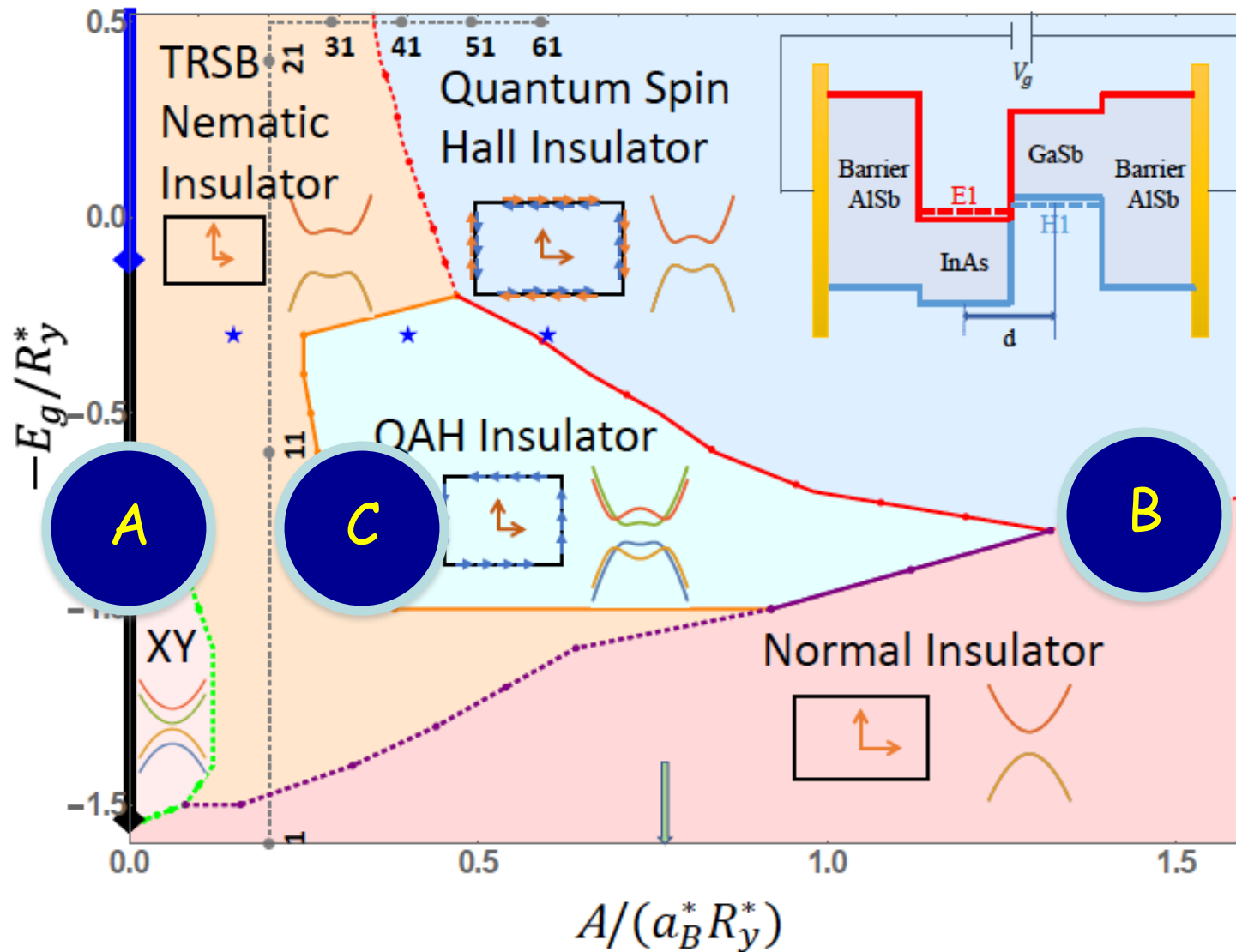
# Gapped States in Bilayer Graphene

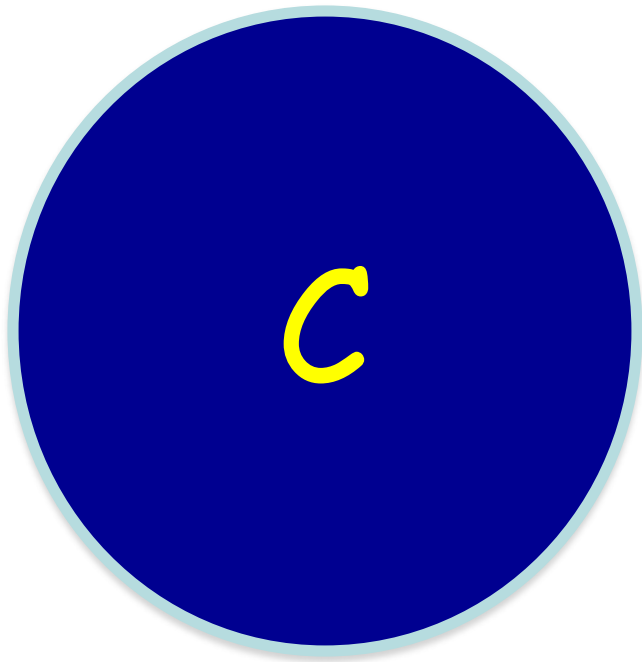


Bao, Velasco Nature Phys. (2011), arXiv:1108



Xue & AHM, arXiv:1710.00410 PRL (2018)





# Nematic and Chern Insulators

# Excitonic Insulator to BHZ model

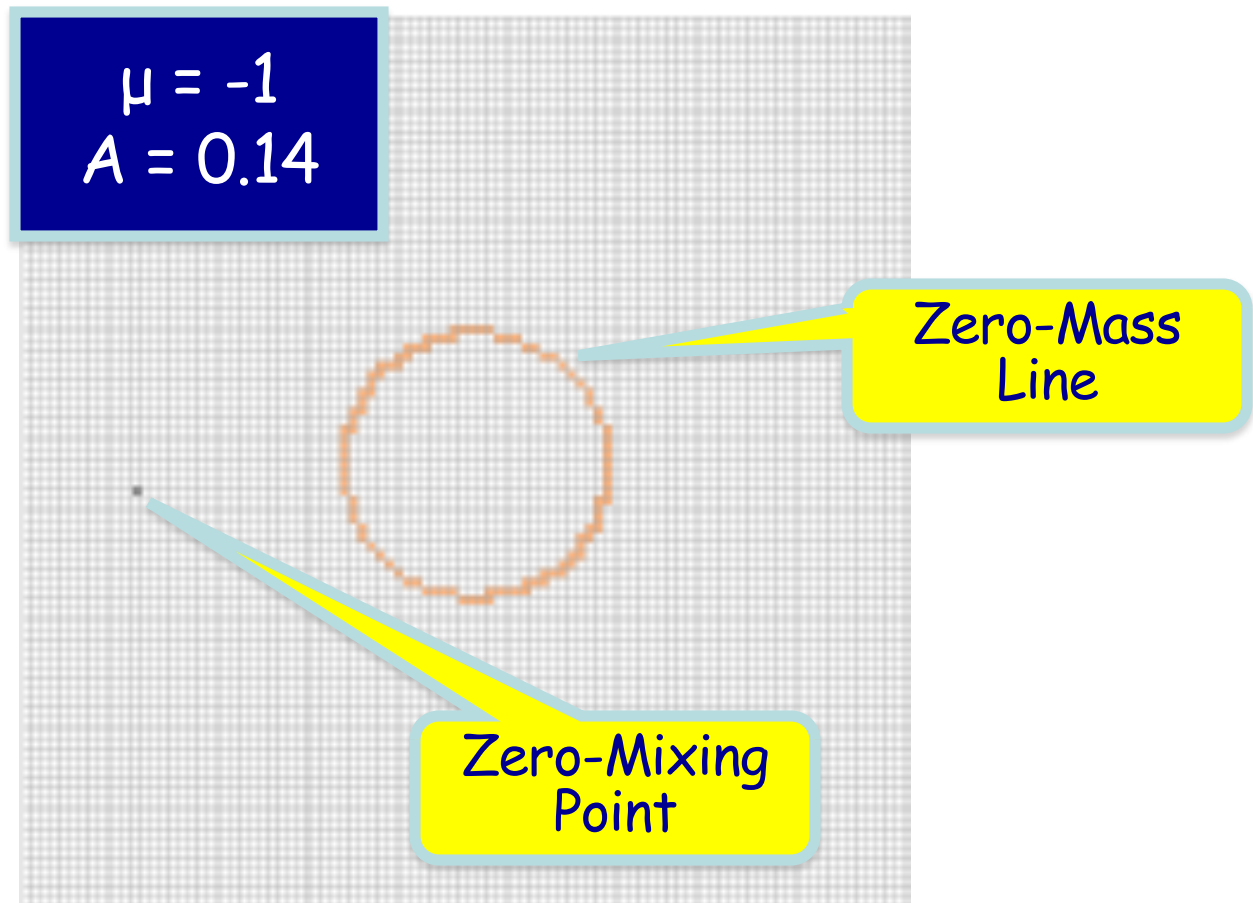
k-dependent  
gap

$$\mathcal{H}_{\text{BHZ}} = \left( \frac{\hbar^2 k^2}{2m} + \frac{E_{\text{gap}}}{2} \right) \tau_z + A(k_x \tau_x \sigma_z - k_y \tau_y)$$

k-dependent  
Band-Pseudospin  
Effective Magnetic  
Field

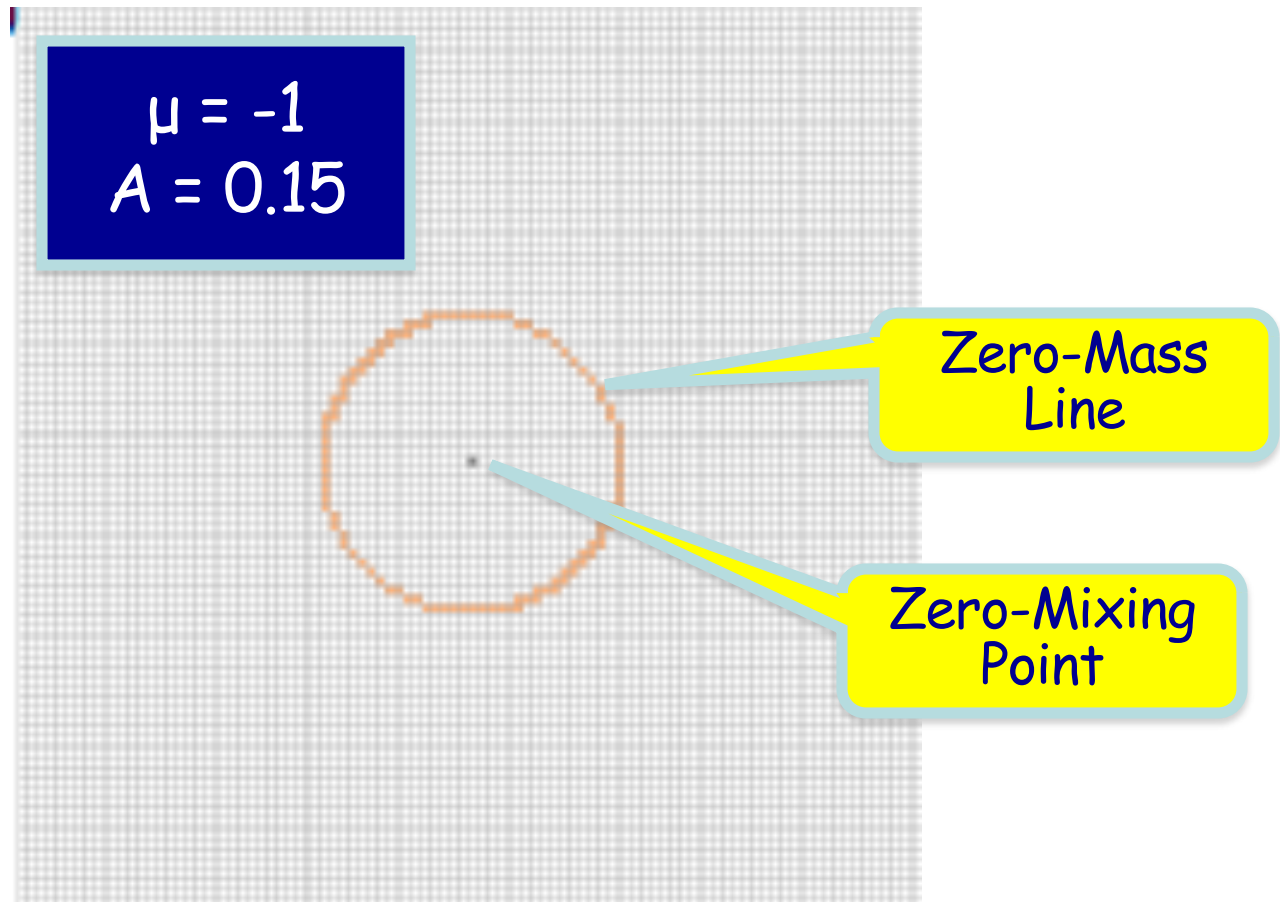
# Mean-Field Theory - QSHI/NI

Nematic Insulator

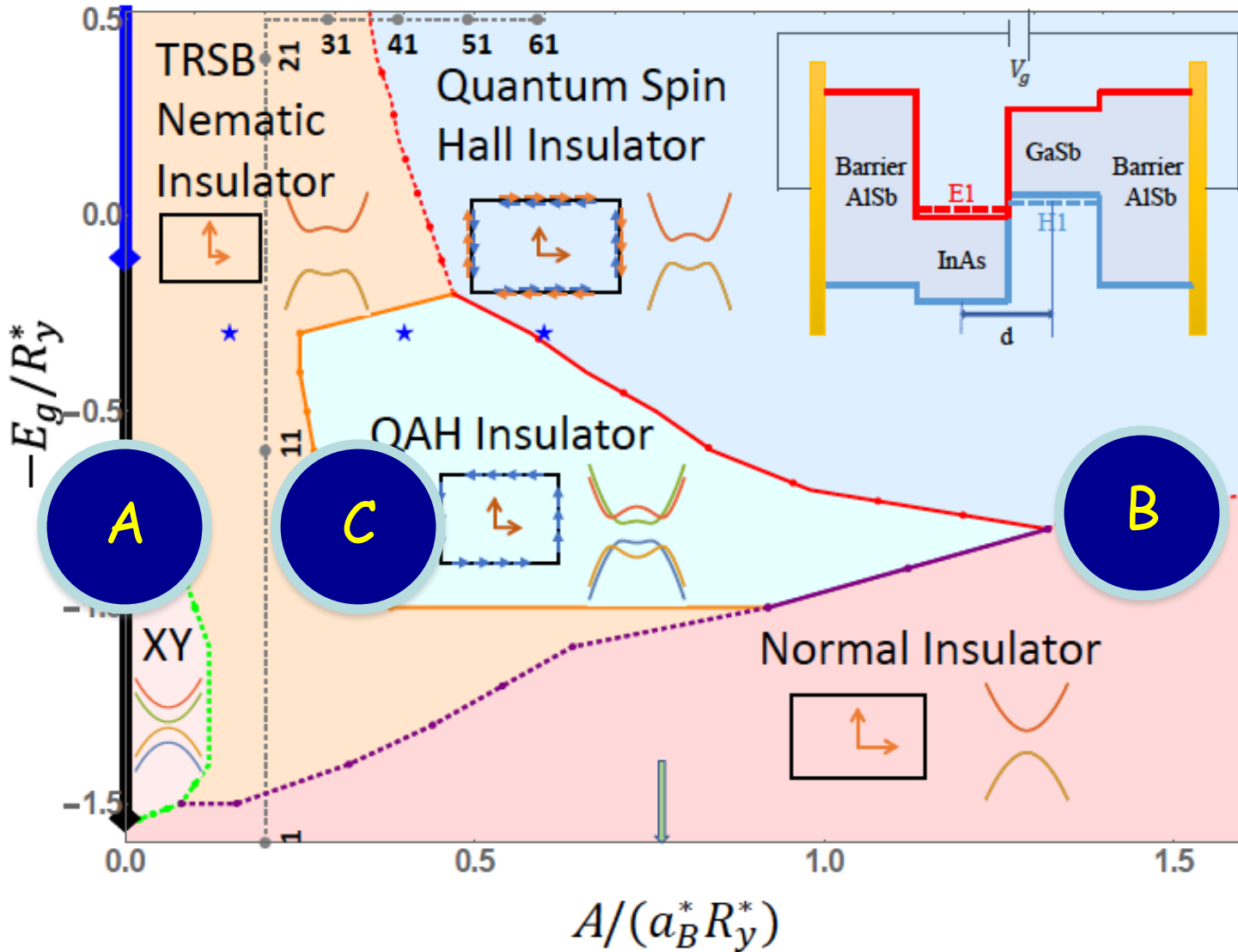


# Mean-Field Theory - QSHI/NI

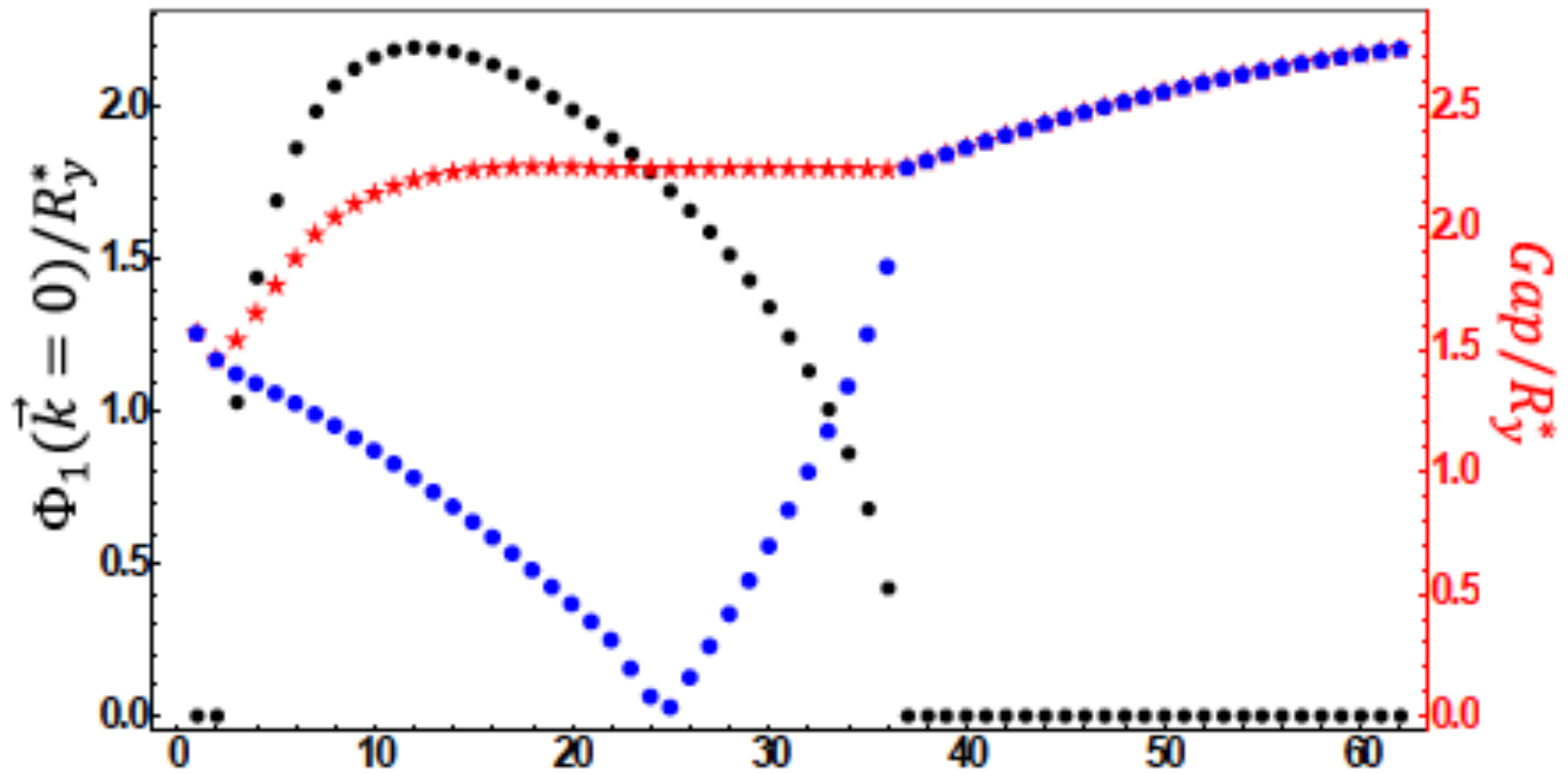
QSH Insulator

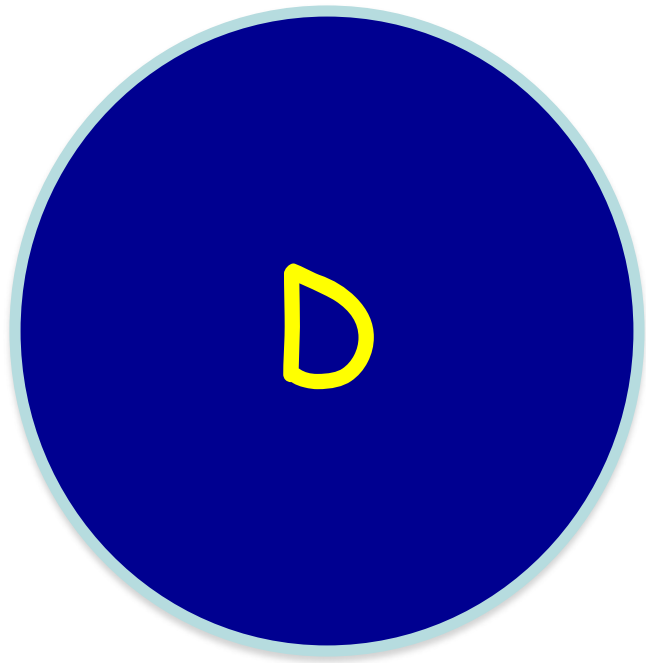


Xue & AHM, arXiv:1710.00410 PRL (2018)



# Mind the Gap

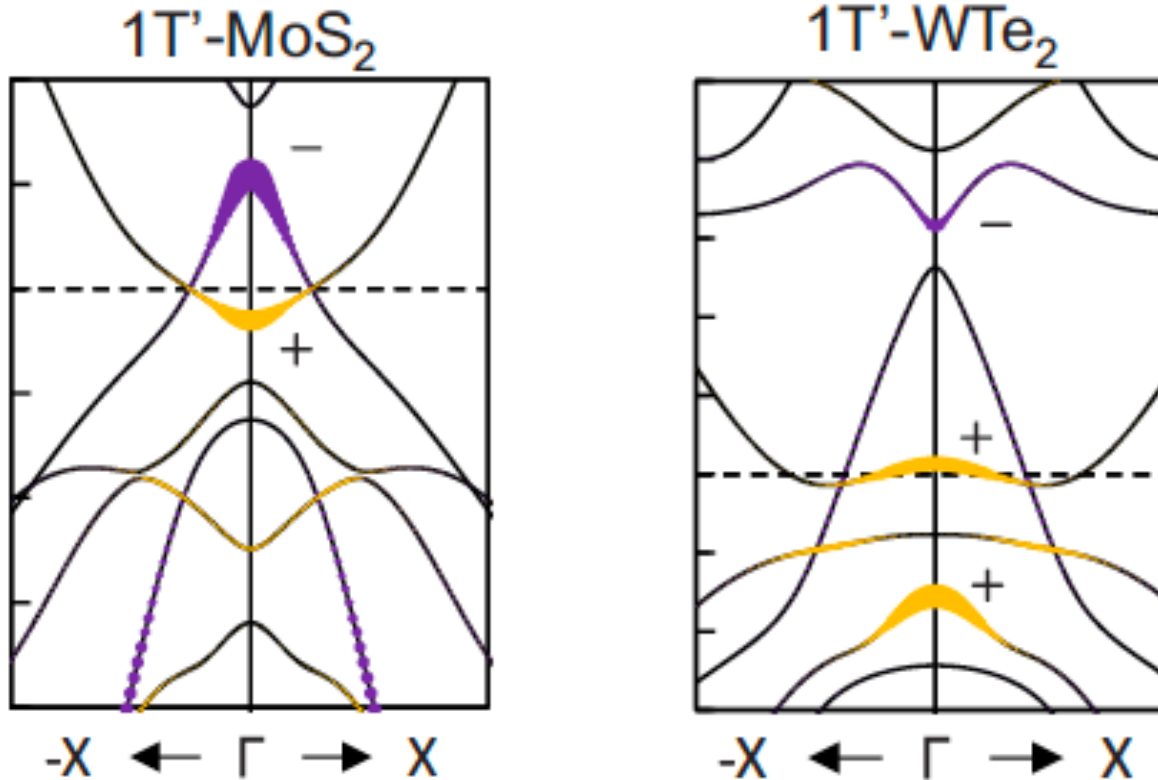




Less Simple  
Systems



# The 1T' TMDs



Qian et al. *Science* (2014)  
Choe et al. *PRB*, 93, 125109 (2016)  
Meuchler et al. *PRX*, 6, 041069 (2016)

- ✓ The Coulomb interaction's long range must be retained in the theory of interaction effects in semiconductors and semi-metals and are often accurately described by *GW* approximations
- ✓ Broken Symmetries are Common in weakly correlated semiconductors and semimetals - especially in candidate topological materials

Electronic Structure 2018

---

# *Interaction Physics in Semimetals*

Fei Xue Fengcheng Wu  
Juanjo Palacios AHM

The University of Cambridge

